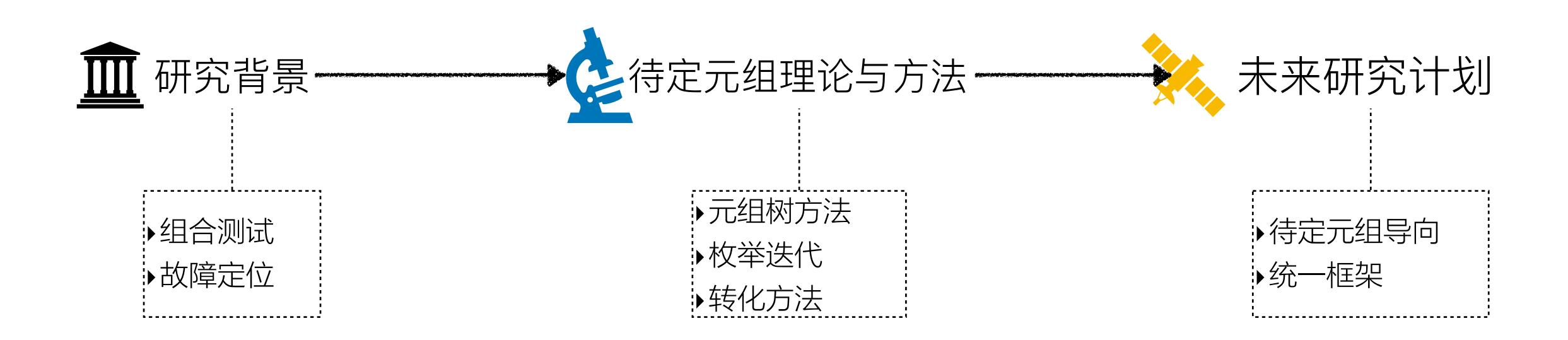




# 组合测试中的故障定位

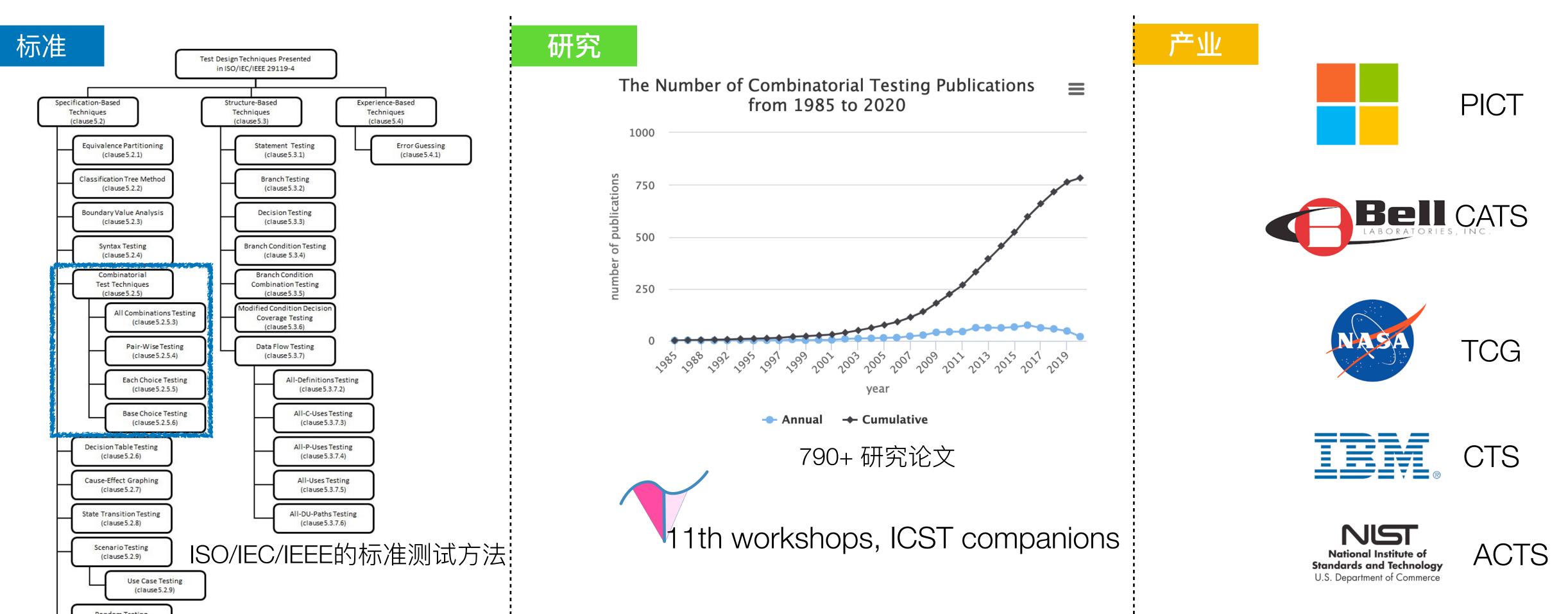
钮鑫涛 2022.11.03

#### 提纲



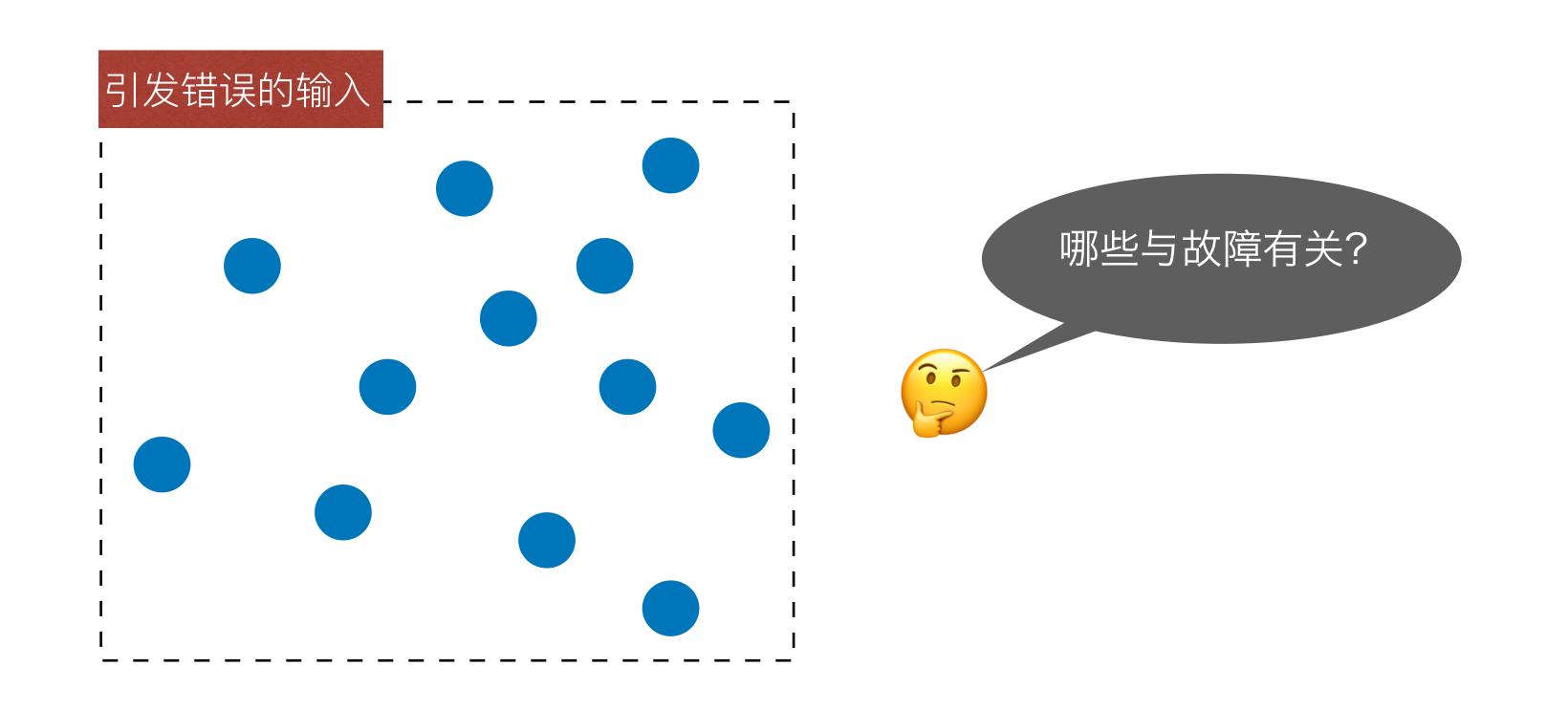
#### 研究背景-组合测试

● 组合测试是一种测试"因素"之间组合的一种黑盒测试方法。



# 组合测试故障定位问题

● 一条出错的测试输入中,哪些是导致这次错误的关键因素(组合)?



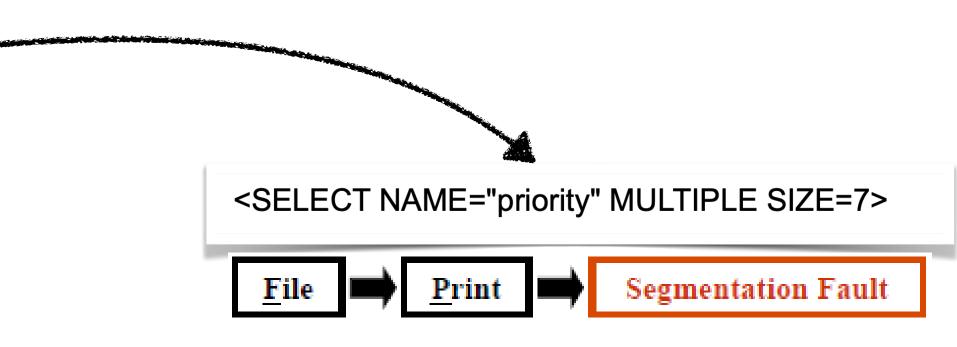
#### 问题普遍性

#### Mozilla Bug #24735

```
<SELECT NAME="op sys" MULTIPLE SIZE=7>
<OPTION VALUE="All">All<OPTION VALUE="Windows 3.1">Windows 3.1<OPTION VALUE="Windows 95">Windows
95<OPTION
VALUE="Windows 98">Windows 98<OPTION VALUE="Windows ME">Windows ME<OPTION VALUE="Windows 2000">Windows
2000<OPTION VALUE="Windows NT">Windows NT<OPTION VALUE="Mac System 7">Mac System 7<OPTION VALUE="Mac
System
7.5">Mac System 7.5<OPTION VALUE="Mac System 7.6.1">Mac System 7.6.1<OPTION VALUE="Mac System 8.0">Mac System
8.0<OPTION VALUE="Mac System 8.5">Mac System 8.5<OPTION VALUE="Mac System 8.6">Mac System 8.6<OPTION
VALUE="Mac
System 9.x">Mac System 9.x<OPTION VALUE="MacOS X">MacOS X<OPTION VALUE="Linux">Linux<OPTION
VALUE="BSDI">BSDI<OPTION VALUE="FreeBSD">FreeBSD<OPTION VALUE="NetBSD">NetBSD<OPTION
VALUE="OpenBSD">OpenBSD<OPTION VALUE="AIX">AIX<OPTION VALUE="BeOS">BeOS<OPTION VALUE="HP-
UX">HPUX<
OPTION VALUE="IRIX">IRIX<OPTION VALUE="Neutrino">Neutrino<OPTION VALUE="OpenVMS">OpenVMS<OPTION
VALUE="OS/2">OS/2<OPTION VALUE="OSF/1">OSF/1<OPTION VALUE="Solaris">Solaris<OPTION
VALUE="SunOS">SunOS<OPTION VALUE="other">other</SELECT>
<SELECT NAME="priority" MULTIPLE SIZE=7>
<OPTION VALUE="--">--<OPTION VALUE="P1">P1<OPTION VALUE="P2">P2<OPTION VALUE="P3">P3<OPTION</pre>
VALUE="P4">P4<OPTION VALUE="P5">P5</SELECT>
<SELECT NAME="bug severity" MULTIPLE SIZE=7>
<OPTION VALUE="blocker">blocker<OPTION VALUE="critical">critical<OPTION VALUE="major">major<OPTION</p>
VALUE="normal">normal<OPTION VALUE="minor">minor<OPTION VALUE="trivial">trivial<OPTION
VALUE="enhancement">enhancement<
```

Segmentation Fault

Print 📥



#### 问题普遍性

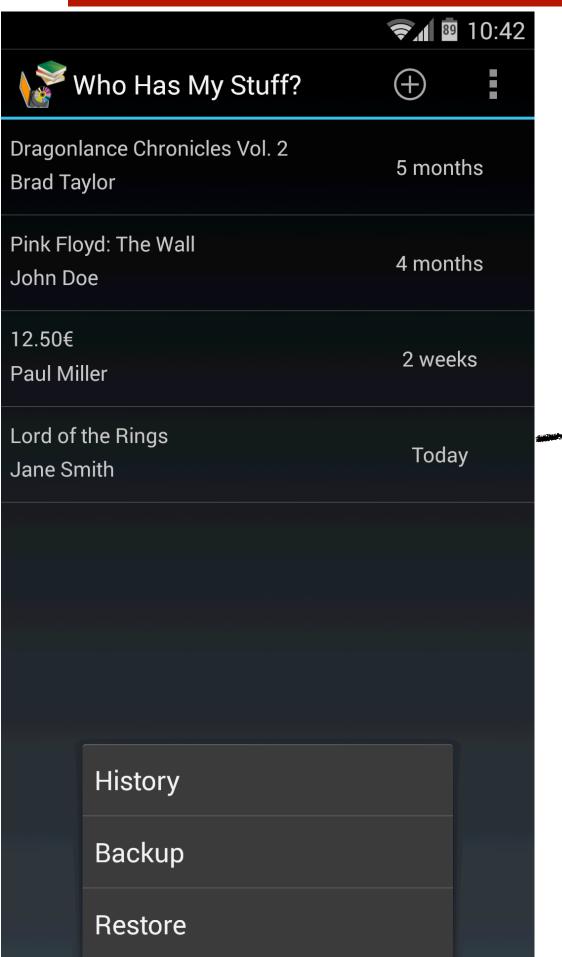
#### Gcc 2.59.2 with optimization

```
#define SIZE 20
double mult(double z[], int n)
    int i, j;
    i = 0;
    for (j = 0; j < n; j++){
       i = i + j + 1;
       z[i] = z[i] * (z[0] + 1.0);
    return z[n];
 void copy(double to[], double from[], int count)
    int n = (count + 7) / 8;
    switch (count % 8) do
    case 0: *to++ = *from++;
    case 7: *to++ = *from++;
    case 6: *to++ = *from++;
    case 5: *to++ = *from++;
    case 4: *to++ = *from++;
    case 3: *to++ = *from++;
    case 2: *to++ = *from++;
    case 1: *to++ = *from++;
    } while (--n > 0);
    return mult(to, 2);
 int main(int argc, char * argv[])
    double x[SIZE], y[SIZE];
    double *px = x;
    while(px < x + SIZE)
        *px++ = (px -x) * (SIZE +1.0);
    return copy(y, x, SIZE);
```

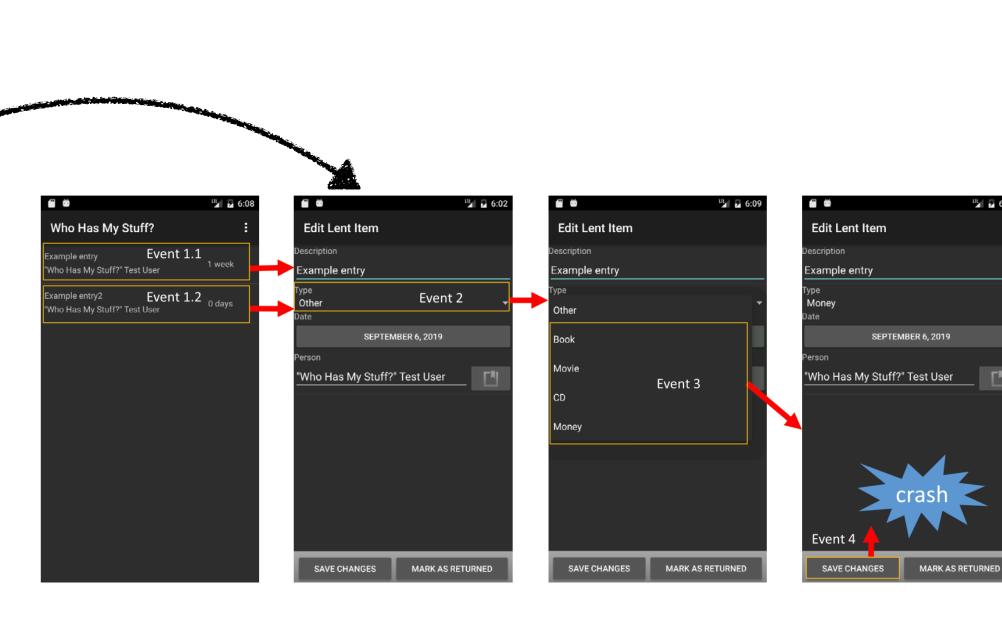
```
1 t(double z[], int n){int i,j;for(;;){i=i+j+1;z[i]=z[i]*(z[0]+0);}return z[n];}
```

### 问题普遍性

#### APP—Who has my stuff?



```
#1: Switch: Component = de.freewarepoint.whohasmystuff/.ListLentObjects
#2: Sending Touch (ACTION_DOWN): 0:(127.0, 1353.0)
#3: Sending Touch (ACTION_UP): 0:(122.13759, 1337.722)
Sleeping for 800 milliseconds
#8: Sending Touch (ACTION_DOWN): 0:(539.0, 434.0)
#9: Sending Touch (ACTION_UP): 0:(533.3379, 434.0376)
Sleeping for 800 milliseconds
#14: Sending Touch (ACTION_DOWN): 0:(117.0, 912.0)
#15: Sending Touch (ACTION_UP): 0:(117.86061, 895.20026)
Sleeping for 800 milliseconds
#18: Sending Touch (ACTION_DOWN): 0:(344.0, 164.0)
#19: Sending Touch (ACTION_UP): 0:(345.1393, 163.97989)
Sleeping for 800 milliseconds
#60: Sending Touch (ACTION_DOWN): 0:(1027.0, 292.0)
#61: Sending Touch (ACTION_UP): 0:(1023.24646, 287.6247)
Sleeping for 800 milliseconds
#96: Sending Touch (ACTION_DOWN): 0:(247.0, 763.0)
#97: Sending Touch (ACTION_UP): 0:(253.49065, 758.454)
Sleeping for 800 milliseconds
#98: Sending Touch (ACTION_DOWN): 0:(300.0, 1594.0)
#99: Sending Touch (ACTION_UP): 0:(299.41364, 1583.6807)
Sleeping for 800 milliseconds
#142: Sending Touch (ACTION_DOWN): 0:(271.0, 504.0)
#143: Sending Touch (ACTION_UP): 0:(273.97485, 499.46576)
Sleeping for 800 milliseconds
#144: Sending Touch (ACTION_DOWN): 0:(595.0, 1229.0)
#145: Sending Touch (ACTION_UP): 0:(590.3204, 1218.4806)
Sleeping for 800 milliseconds
#146: Sending Touch (ACTION_DOWN): 0:(326.0, 1812.0)
#147: Sending Touch (ACTION_UP): 0:(334.20886,1806.3463)
```



Monkey sequence (147 events)

#### 问题的重要性



故障定位占据了50%以上的测试成本 [Judge Business School 2013]



触发故障的关键因素 [Nie 2011]



可以有效减少代码审查的范围 [Ghandehari 2012]



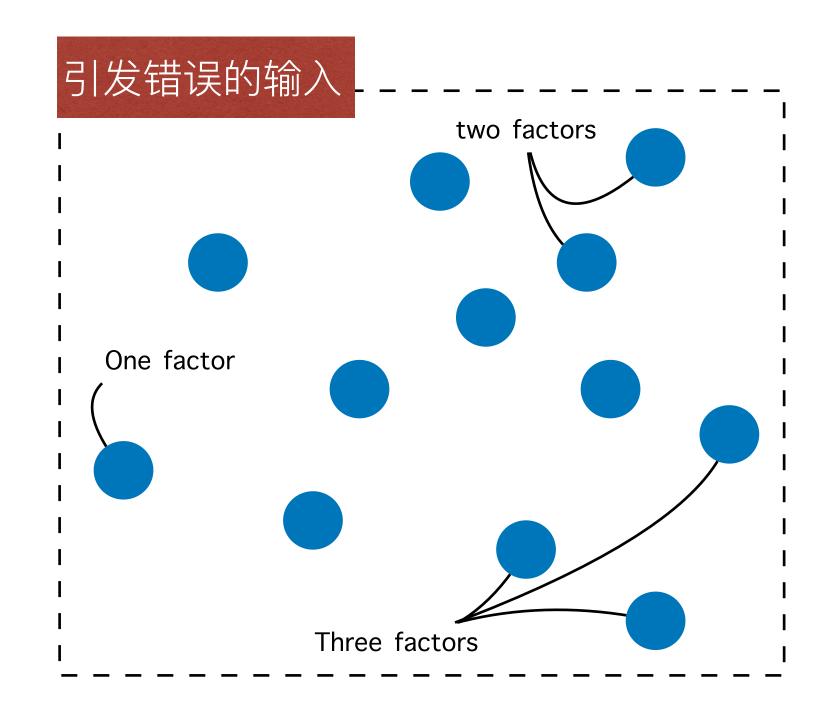
避免重复故障报告 [Zeller 2002]



有利于进一步的修复工作 [Song 2012]

### 组合测试故障定位难度

- 一般地,当系统的参数个数为n时,一条触发故障的测试用例可能的故障元组个数是 $2^n 1$ 个。
  - 巨大的解空间对故障定位方法造成了非常大的挑战!



共有
$$\binom{n}{1}$$
 +  $\binom{n}{2}$  +  $\cdots$  +  $\binom{n}{n}$  =  $2^n - 1$ 可能的故障元组

### 已有代表性工作

IEEE TRANSACTIONS ON SOFTWARE ENGINEERING, VOL. 28, NO. 2, FEBRUARY 2002

#### Simplifying and Isolating Failure-Inducing

Andreas Zeller, Member, IEEE Computer Society, and Ralf Hildebrandt

Abstract—Given some test case, a program fails. Which circumstances of the test case are responsible for the particular Delta Debugging algorithm generalizes and simplifies the failing test case to a minimal test case that still produces the isolates the difference between a passing and a failing test case. In a case study, the Mozilla web browser crashed af actions. Our prototype implementation automatically simplified the input to three relevant user actions. Likewise, it simple of HTML to the single line that caused the failure. The case study required 139 automated test runs or 35 minutes on a

Index Terms—Automated debugging, debugging aids, testing tools, combinatorial testing, diagnostics, tracing.

#### INTRODUCTION

Often people who encounter a bug spend a lot of time investigating which changes to the input file will make the bug go away and which changes will not affect it. —Richard Stallman, Using and Porting GNU CC.

**T**F you browse the Web with Netscape 6, you actually use a ▲variant of Mozilla, Netscape's open source web browser project [1]. As a work in progress with big exposure, the Mozilla project receives several dozens of bug reports a day. The first step in processing any bug report is simplification, that is, eliminating all details that are irrelevant for producing the failure. Such a simplified bug report not only facilitates debugging, but it also subsumes several other bug reports that only differ in irrelevant details.

In July 1999, Bugzilla, the Mozilla bug database, listed more than 370 open bug reports—bug reports that were not one, so far, has thought to automate the even simplified. With this queue growing further, the textbooks and guides about debugging a Mozilla engineers "faced imminent doom" [2]. Over- tell how to use binary search in orde whelmed with work, the Netscape product manager sent problem—based on the assumption that out the Mozilla BugAThon call for volunteers [2]: people who would help process bug reports. For five bug reports simplified, a volunteer would be invited to the launch party; 20 bugs would earn her or him a T-shirt signed by the grateful engineers. "Simplifying" meant turning these bug reports into minimal test cases, where every part of the input case is reached, where removing any sir would be significant in reproducing the failure.

As an example, consider the HTML input in Fig. 1. Loading this HTML page into Mozilla and printing it causes few seconds after taking off. By repeating t a segmentation fault. Somewhere in this HTML input is and over again under changed circumstar something that makes Mozilla fail—but where? If we were out what is relevant and what not. For i Netscape programmers, what we wanted here is the remove the passenger seats and find the simplest HTML page that still produces the failure.

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- E-mail: zeller@computer.org.
  R. Hildebrant is with DeTeLine Deutsche Telekom Kommunikationsnetze GmbH, Rognitzstrasse 9, 14057 Berlin, Germany.
- Manuscript received Mar. 2001; revised June 2001; accepted July 2001. Recommended for acceptance by M.J. Harrold and A. Bertolino. For information on obtaining reprints of this article, please send e-mail to: tse@computer.org, and reference IEEECS Log Number 115156.

[Zeller et al 2002 TSE]

Decomposing specific bug reports into does not trouble only the Mozilla enginee arises from generally conflicting issues:

- A bug report should be as specific that the engineer can recreate the the program failed.
- On the other hand, a test case shou possible because a minimal test cas general context.

Thus, a minimal test case not only allows f descriptions and valuable problem insisubsumes several current and future bug The striking thing about test case simpli-

automate this simplification of test case automatically isolate the difference that cause Simplification of test cases. Our minimizin

algorithm ddmin is fed with a failing tes simplifies by successive testing. It stops wh would cause the failure to disappear. As a the real world, consider a flight test: An ai crashes. We may remove the coffee machistill crashes. Eventually, only the relev skeleton remains, including a test pilot, runway, the fuel, and the engines. Each par is relevant for reproducing the crash. In the one with a sane mind would consider simplify the circumstances of test flight simulations of flight tests or, more genera computer programs, such an approach con cost. The cost may be so low that we can e

amount of tests just to simplify a test case

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#### LOCATING ERRORS USING ELAS, COVERING ARRAYS ADAPTIVE TESTING ALGORITHMS\*

CONRADO MARTÍNEZ<sup>†</sup>, LUCIA MOURA<sup>‡</sup>, DANIEL PANARIO<sup>§</sup>, AND BRETT

Abstract. In this paper, we define and study error locating arrays (ELAs), which n software testing for locating faulty interactions among parameters or components We give constructions of ELAs for arbitrary strength t, based on covering arrays. We si number of tests given by ELAs grows as  $O(\log k)$ , where k is the number of parameters/co the system, assuming other quantities (the number g of values per parameter, the streng interactions, and the number d of faulty interactions) are bounded by a constant. We series of results for the case of pairwise interactions (t = 2). We study the computational of deciding whether a graph describing the faulty pairwise interactions is "locatable." We the locatable graphs for the binary case (g = 2). We design and analyze efficient algorithms. locate errors under certain assumptions on the structure of the faulty pairwise interact the assumption of known "safe values," our algorithm performs a number of tests that i in  $\log k$  and d, where k is the number of parameters in the system and d is an upper b number of faulty pairwise interactions. For the binary alphabet case, we provide an al does not require safe values and runs in expected polynomial time in  $\log k$  whenever  $d \in$ 

Key words. combinatorial designs, covering arrays, error locating arrays, letecting arrays, algorithms, software testing, component interaction testing, group test

AMS subject classifications. 94C30, 05B30, 94C12, 05C99

DOI. 10.1137/080730706

1. Introduction. Consider a complex system whose behavior depen values of k parameters or factors. To temporarily simplify matters, support the k factors may take any of two values. In order to exhaustively test the tests are required, rendering it infeasible in a practical setting, even when

An alternative to exhaustive testing is provided by covering arrays binary CA is a 0-1 matrix with n rows and k columns. Each of its columns a parameter and each of its rows gives a test to be performed. The numb n is called the size of the array. The array is said to be of strength t if subset of the k factors, the corresponding columns exhaustively cover all combinations. In other words, if we define a t-way interaction to be the of specific values to each factor of a set of t factors, a covering array tests interaction in some of its rows. Since in many practical settings it is enough or 4-way interactions, we can tackle these problems with a moderately

\*Received by the editors July 19, 2008; accepted for publication (in revised form) Ju published electronically December 4, 2009. Part of this research was done while the was on sabbatical leave at Carleton University and later while the second and third aut sabbatical leave at Univ. Politècnica de Catalunya.

http://www.siam.org/journals/sidma/23-4/73070.html

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§School of Mathematics and Statistics, Carleton University, Ottawa, ON, K1S 5B6, Canada (daniel@math.carleton.ca, brett@math.carleton.ca). The third author was supported by NSERC and the Spanish Min. of Education and Science. The fourth author was supported by NSERC, CFI, OIT, and Ontario MRI.

#### The Minimal Failure-Causing Schema of Combinatorial Testir

CHANGHAI NIE, State Key Laboratory for Novel Software Technology, Nanjing Universit HARETON LEUNG, Hong Kong Polytechnic University

Combinatorial Testing (CT) involves the design of a small test suite to cover the parameter tions so as to detect failures triggered by the interactions among these parameters. To make and to extend its advantages, this article first gives a model of CT and then presents a theory o Failure-causing Schema (MFS), including the concept of the MFS, proof of its existence, some ties, and a method of finding the MFS. Then we propose a methodology for CT based on this MI the existing research. Our MFS-based methodology emphasizes that CT should work on acc requirements, and has the following advantages: 1) Detect failure to the greatest degree with 2) Effectiveness is improved by emphasizing mining of the information in software and make the information gained from test design and execution. 3) Determine the root causes of failur related faults near the exposed ones. 4) Provide a foundation and model for regression testing quality evaluation of CT. A case study is presented to illustrate the MFS-based CT method empirical study on a real software developed by us shows that the MFS really exists and the based on MFS can considerably improve CT.

Categories and Subject Descriptors: D.2.5 [Software Engineering]: Testing and Debugging-D.2.4 [Software Engineering]: Software/Program Verification

General Terms: Experimentation, Verification

Additional Key Words and Phrases: Combinatorial testing (CT), Minimal failure-causing so

#### ACM Reference Format:

Nie, C. and Leung, H. 2011. The minimal failure-causing schema of combinatorial testing. Softw. Eng. Methodol. 20, 4, Article 15 (September 2011), 38 pages. DOI = 10.1145/2000799.2000801 http://doi.acm.org/10.1145/2000799.2000801

In software testing, if we know that there are some factors with mutual i that may affect the software under test, it is logical to test with a test suite these factors and their interactions. However, in such cases the necessary t generally too large, making exhaustive testing usually impractical and off ble. Consequently, we need to make a trade-off between testing efficiency an

This work was supported in part by the National Natural Science Foundation of China (607731 90818027), 863 high technical plan of China (2008AAO1Z143, 2009AAO1Z147). This article was partly written during C. Nie's sabbatical in CREST (Center for Research

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DOI 10.1145/2000799.2000801 http://doi.acm.org/10.1145/2000799.2000801

#### Characterizing Failure-Causing Parameter Interactions Adaptive Testing\*

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Combinatorial testing is a widely used black-box testing technique, which is used to detect failures caused by parameter interactions (we call them faulty interactions). Traditional combinatorial testing techniques provide fault detection, but most of them provide weak fault diagnosis. In this paper, we propose a new fault characterization method called faulty interaction characterization (FIC) and its binary search alternative FIC\_BS to locate one failure-causing interaction in a single failing test case. In addition, we provide a tradeoff strategy of locating multiple faulty interactions in one test case. Our methods are based on adaptive black-box testing, in which test cases are generated based on outcomes of previous tests. For locating a t-way faulty interaction, the number of test cases used is at most k (for FIC) or  $t(\lceil \log_2 k \rceil + 1) + 1$  (for FIC\_BS), where k is the number of parameters. Simulation experiments show that our method needs smaller number of adaptive test cases than most existing methods for locating randomly-generated faulty interactions. Yet it has stronger or equivalent ability of locating

#### Categories and Subject Descriptors

D.2.5 [Software Engineering]: Testing and Debugging-Debugging aids, Testing tools

#### **General Terms**

Algorithms, Reliability

Combinatorial testing, diagnostics, faulty interaction, adaptive testing, group testing

\*This work is supported in part by the National Science Foundation of China (Grant No. 61070039) and the High-Tech (863) program of China (Grant No. 2009AA01Z148).

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#### 1. INTRODUCTION

Assume that we are testing the functionality of whose behavior is affected by k parameters (or ca tors"), an ideal plan is to apply exhaustive testing we test all possible combinations of the paramete ever, the number of test cases of exhaustive test exponentially with k. Suppose each parameter has sible values, then we need  $2^k$  test cases. So it is in to be applied on many large applications. Combinatorial testing is a widely used black-bo

Jian Zhang

State Key Laboratory of Computer Science,

technique, which uses covering arrays (CA) or a ering arrays (MCA) [2] as the test suite to detec caused by parameter interactions. A CA(n; k, t, s)ray of n rows and k columns, where n is the s CA, k is the number of parameters and s is the possible values of each parameter. Each column re parameter and each row represents a test case. The strength t, i.e. for any t columns of the array, the covers all possible combinations of the correspond rameters. MCA is similar to CA, while the only is that parameters may have different number of

The fault model of combinatorial testing assu failures are caused by parameter interactions. A teraction or an interaction of size t is an assigsome specific value to each parameter of selected eters. A failure-causing interaction is called a fau action. Kuhn and Reilly's investigation on softwar [6] stated that failures are always caused by intera small sizes. Although it is not universally true, w focus on this kind of failures in this paper. Since array of strength t covers all t-way interactions, tect all failures caused by faulty interactions of size than t. Moreover, the size of CAs grows logarithmic k [1]. Thus, combinatorial testing is quite resour in practical applications.

After a failure is detected by applying combinat ing, we know that it is caused by a faulty interact failure is actually caused by a bug inside the softw we shall locate the bug before fixing it. There ar research on combinatorial testing in recent years ever, most traditional combinatorial testing techni at increasing interaction coverage and reducing the of test cases, while very few of them focus on diag

Table 1 shows a covering array of strength 2 f an online payment system. The interactions in braA Combinatorial Testing-Based Approach to Fault Localization

Laleh Sh. Ghandehari<sup>®</sup>, Yu Lei<sup>®</sup>, Raghu Kacker, Richard Kuhn<sup>®</sup>, Fellow, IEEE, Tao Xie, Fellow, IEEE, and David Kung

IEEE TRANSACTIONS ON SOFTWARE ENGINEERING, VOL. 46, NO. 6, JUNE 2020

Abstract—Combinatorial testing has been shown to be a very effective strategy for software testing. After a failure is detected, the next task is to identify one or more faulty statements in the source code that have caused the failure. In this paper, we present a fault localization approach, called BEN, which produces a ranking of statements in terms of their likelihood of being faulty by leveraging the result of combinatorial testing. BEN consists of two major phases. In the first phase, BEN identifies a combination that is very likely to be failure-inducing. A combination is failure-inducing if it causes any test in which it appears to fail. In the second phase, BEN takes as input a failure-inducing combination identified in the first phase and produces a ranking of statements in terms of their likelihood to be faulty. We conducted an experiment in which our approach was applied to the Siemens suite and four real-world programs, flex, grep, gzip and sed, from Software Infrastructure Repository (SIR). The experimental results show that our approach can effectively and efficiently localize the faulty statements in these programs.

Index Terms—Combinatorial testing, fault localization, debugging

OMBINATORIAL testing is based on the observation that [8], [29], [33], or demonstrating the effectiveness of combina a large number of software failures are caused by intertorial testing in different application domains [6], [15], [44] actions of only a few input parameters [26]. A t-way combi- [48]. Several approaches have been developed to identify natorial test set, or simply a t-way test set, is designed to failure-inducing combinations in a combinatorial test set cover all the t-way combinations, i.e., combinations involv- [49], [57]. A failure-inducing combination, or simply ar ing any t parameters [8], [9], [29]. Typically, t is a small inducing combination, is a combination that causes all tests number and is referred to as the strength of a combinatorial containing this combination to fail [34], [57]. These test set [25], [26]. When the input parameters are properly approaches, however, are not designed to locate faulty statemodeled, a t-way test set could trigger any failure caused ments in the source code. by interaction of at most t parameters. Empirical studies A significant amount of research has been reported or have shown that combinatorial testing is very effective in spectrum-based approaches to fault localization [1], [23], practice [6], [16], [25].

After a failure is detected during combinatorial testing, certain aspects of a test execution [50], such as function call the next task is locating the fault that caused the failure. In counts, program paths, program slices and use-def chains this paper, we present a fault localization approach called [40]. Examples of spectrum-based methods include Taran BEN that leverages the result of combinatorial testing. BEN tula [24], set union, set intersection, and nearest neighbo takes as input a combinatorial test set and the execution sta- [40]. These approaches identify faulty statements by analyz tus, i.e., pass or fail, of each test, and produces as output a ing the spectra of passing and failing test executions [24] ranking of statements in terms of their likelihood to be [40], [31]. These approaches are not designed to work with Most research in combinatorial testing has focused on lyze test executions obtained from combinatorial testing

developing efficient combinatorial test generation algorithms provided that the test executions were traced. In case that a

- . L. Sh. Ghandehari, Y. Lei and D. Kung are with the Department of Con puter Science and Engineering, University of Texas, Arlington, TX 76019. E-mail: laleh.shikhgholamhosseing@mavs.uta.edu, {ylei, kung}@uta.edu. · R. Kacker, and R. Kuhn are with the Information Technology Lab National Institute of Standards and Technology, Gaithersburg, MD
- 20899. E-mail: {raghu.kacker, kulm}@nist.gov.

  T. Xie is with the Department of Computer Science, North Carolina State

  trast, our approach does not require every test execution to be traced and is designed to be applied after normal testing University, Raleigh, NC 27695. E-mail: taoxie@illinois.edu

Manuscript received 22 Jan. 2016; revised 12 July 2018; accepted 12 July 2018. compare our approach, i.e., BEN, to these approaches both Date of publication 17 Aug. 2018; date of current version 15 June 2020. (Corresponding author: Laleh Sh. Ghandehari.)

Digital Object Identifier no. 10.1109/TSE.2018.2865935

Our approach consists of two major phases, inducing combination identification and faulty statement localization

[40], [50]. A program spectrum records information about

combinatorial testing. However, they can be applied to ana-

mbinatorial test set is already executed without being

traced, which is often the case in practice considering tha

testing and debugging are fundamentally different activitie

and are often performed separately, the test set must be re-

executed before these approaches could be applied. In con-

trast, our approach does not require every test execution to

is performed where test executions are not traced. We will

analytically (Section 6.2) and experimentally (Section 5.2.3)

[Nie et al 2011 TOSEM]

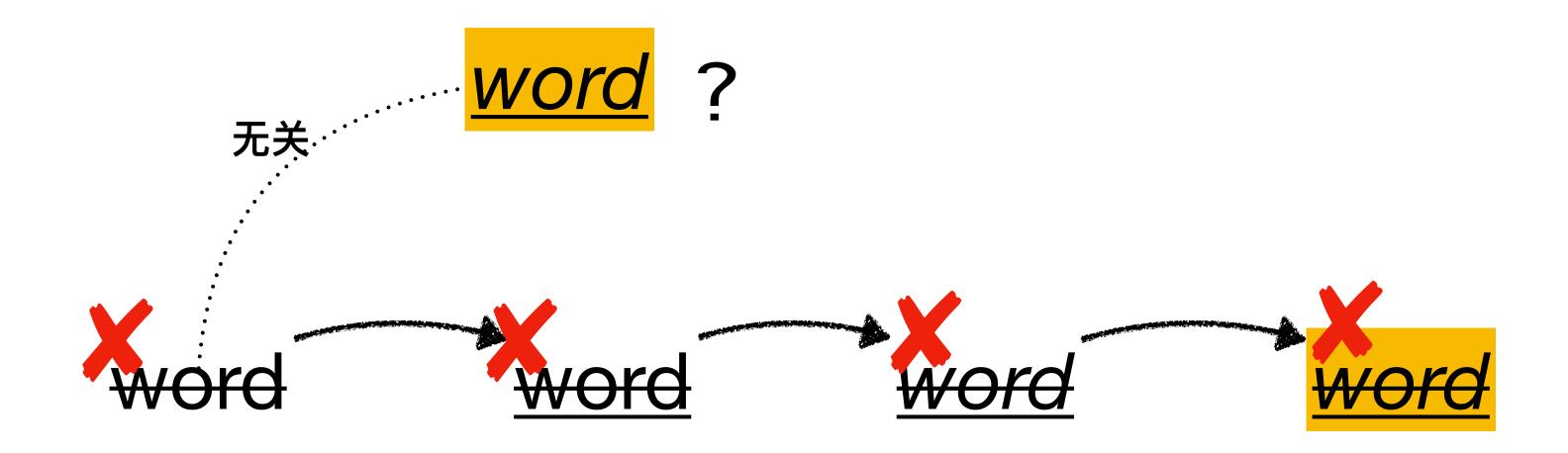
[Zhang 2011 ISSTA]

[Laleh 2020 TSE]

[Mart´ınez et al 2008 SIDMA]

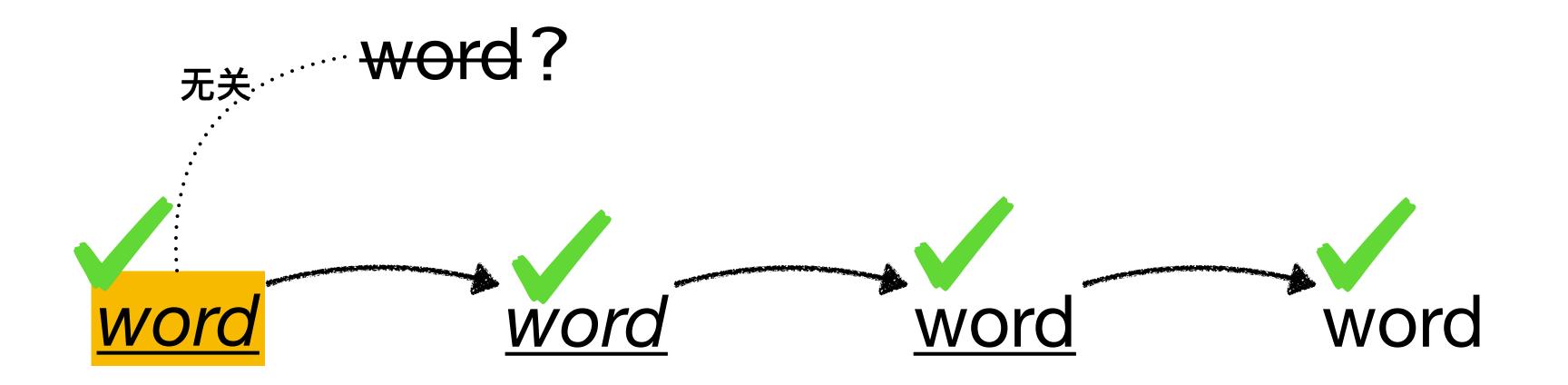
### 基本性质

- 这些方法基于一个基本的性质 (偏序性)
  - 包含故障元组的测试用例(或父元组)一定是故障的!

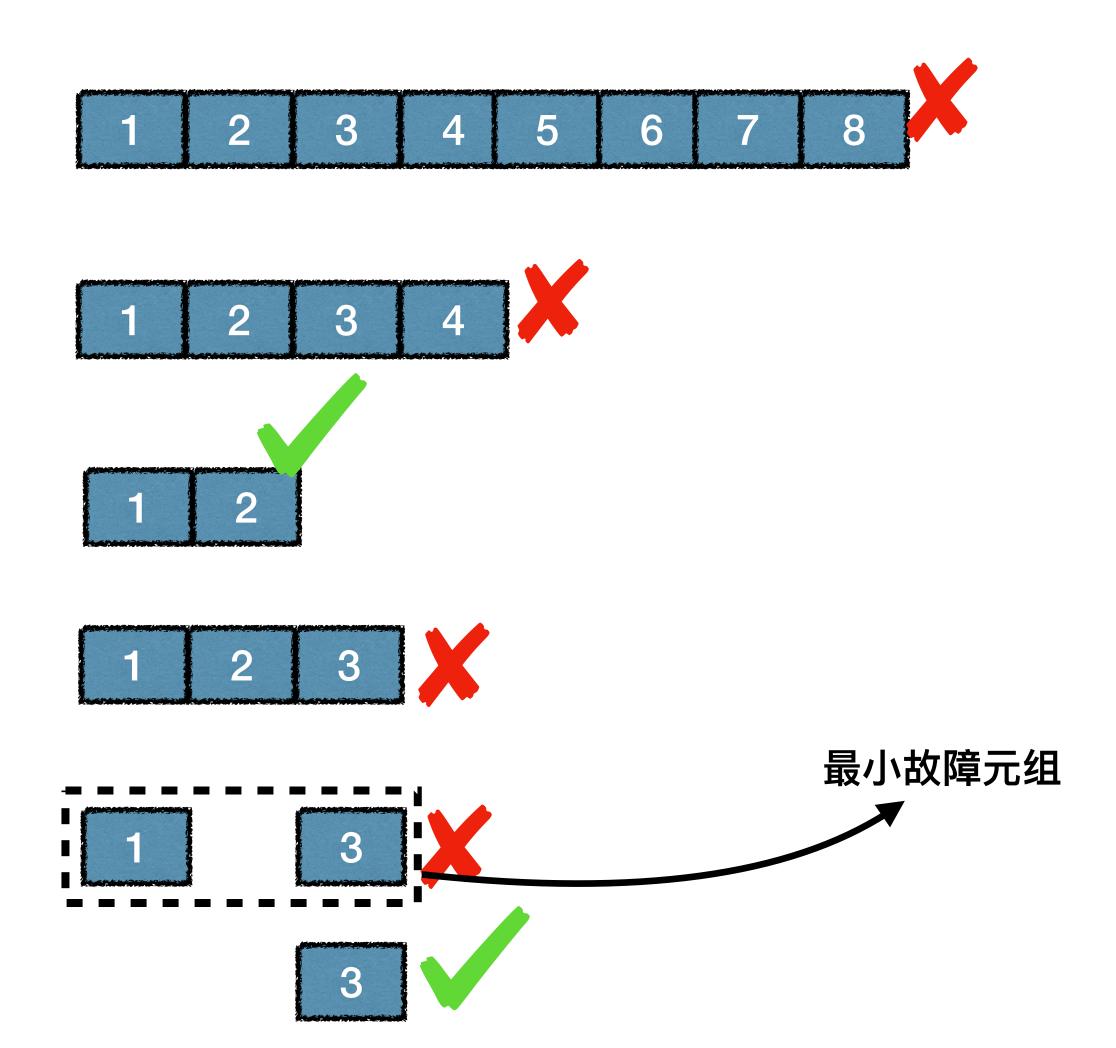


### 基本性质

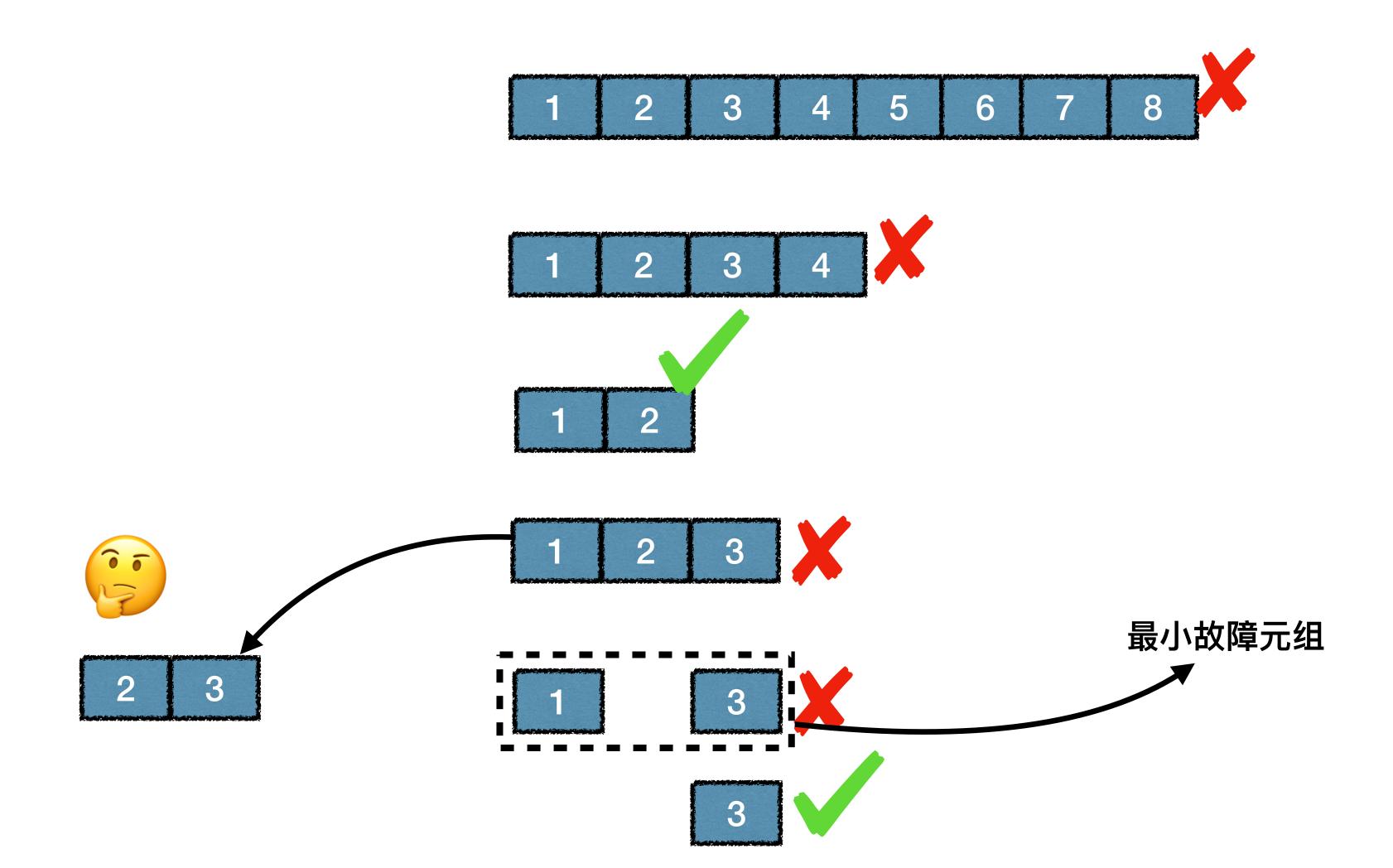
- 上述性质的推论
  - 一条正确的测试用例(或父元组)中的所有子元组都是非故障的! (健康的)

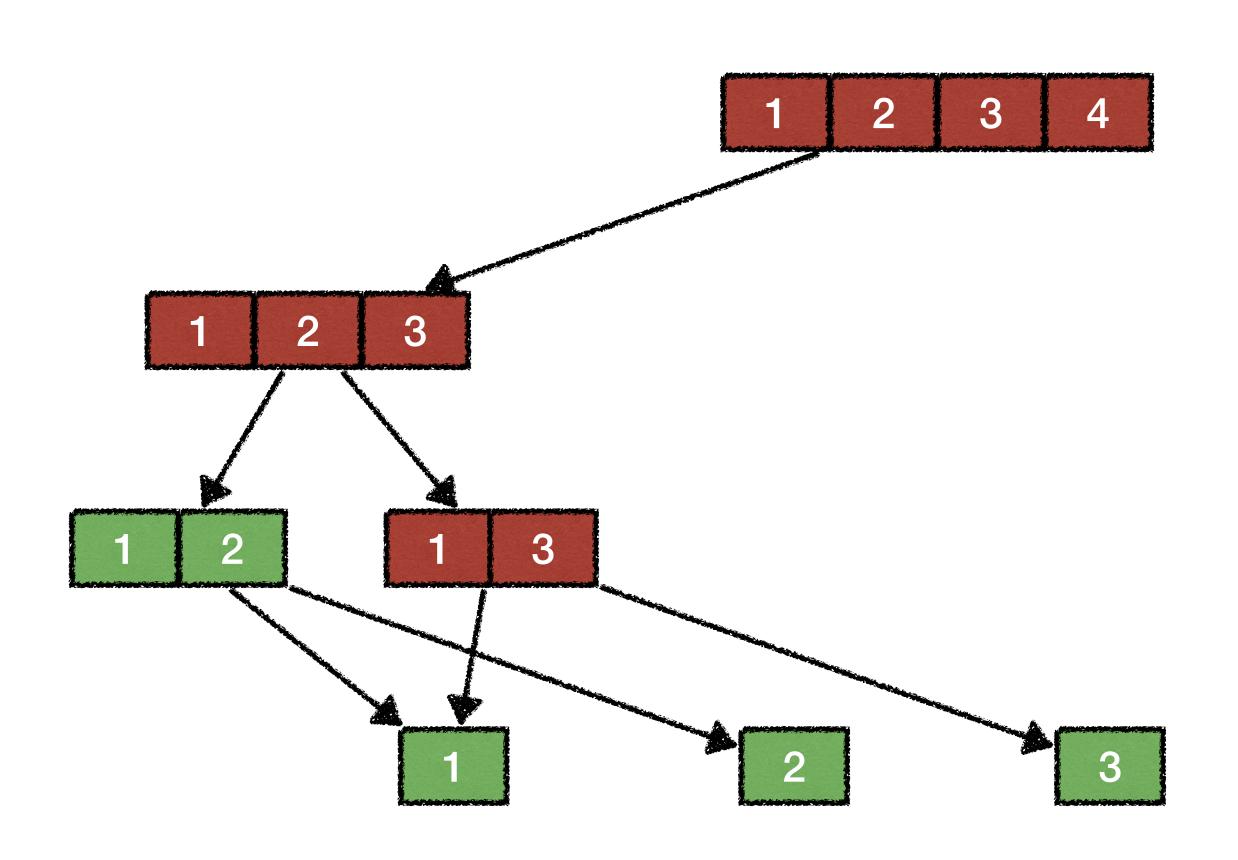


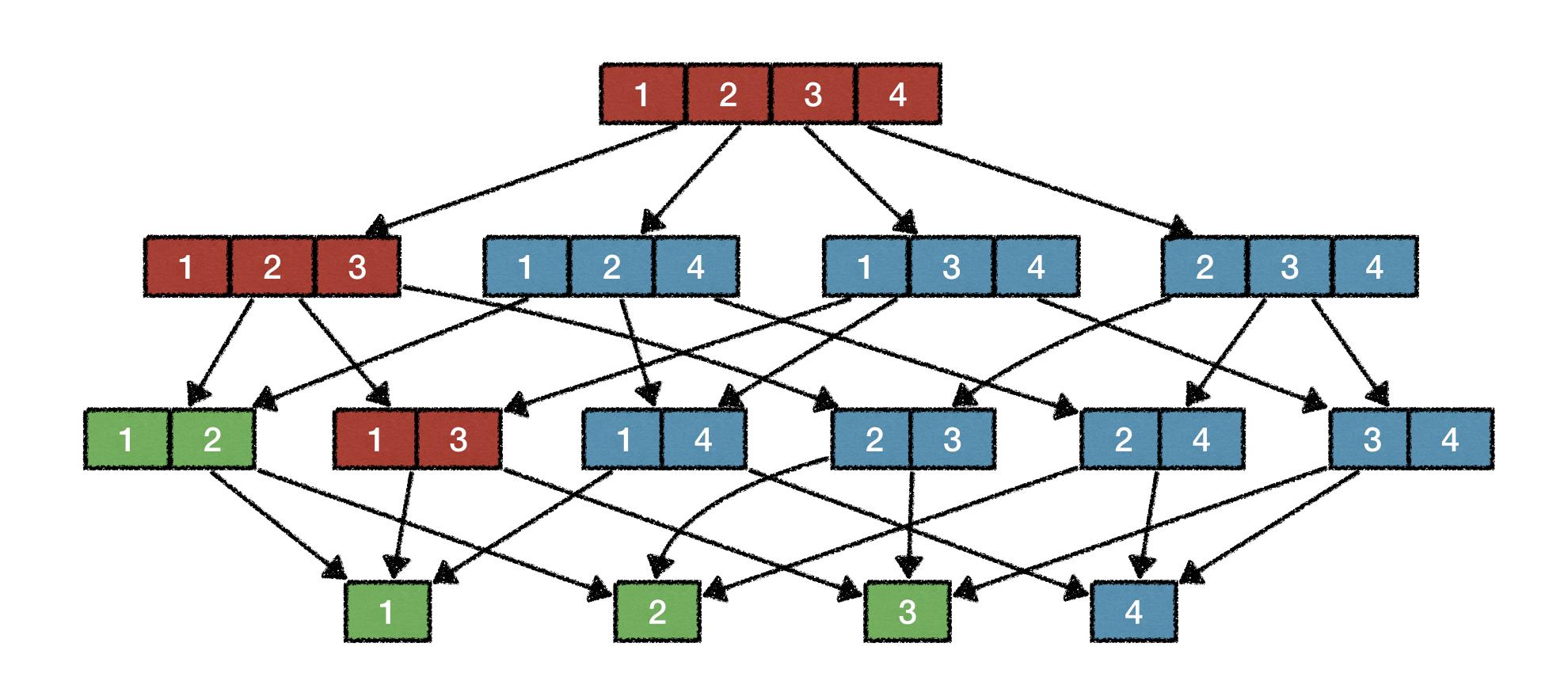
### 组合测试故障定位经典框架

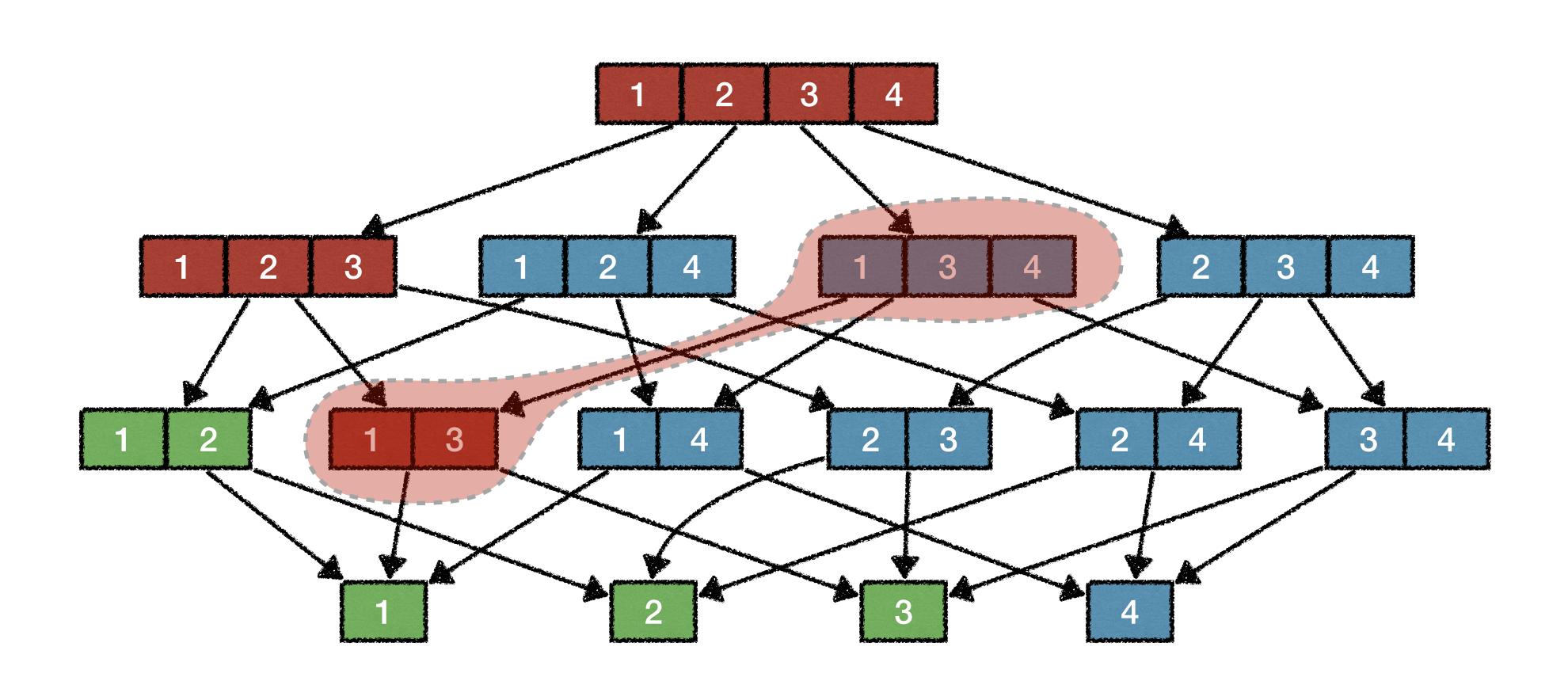


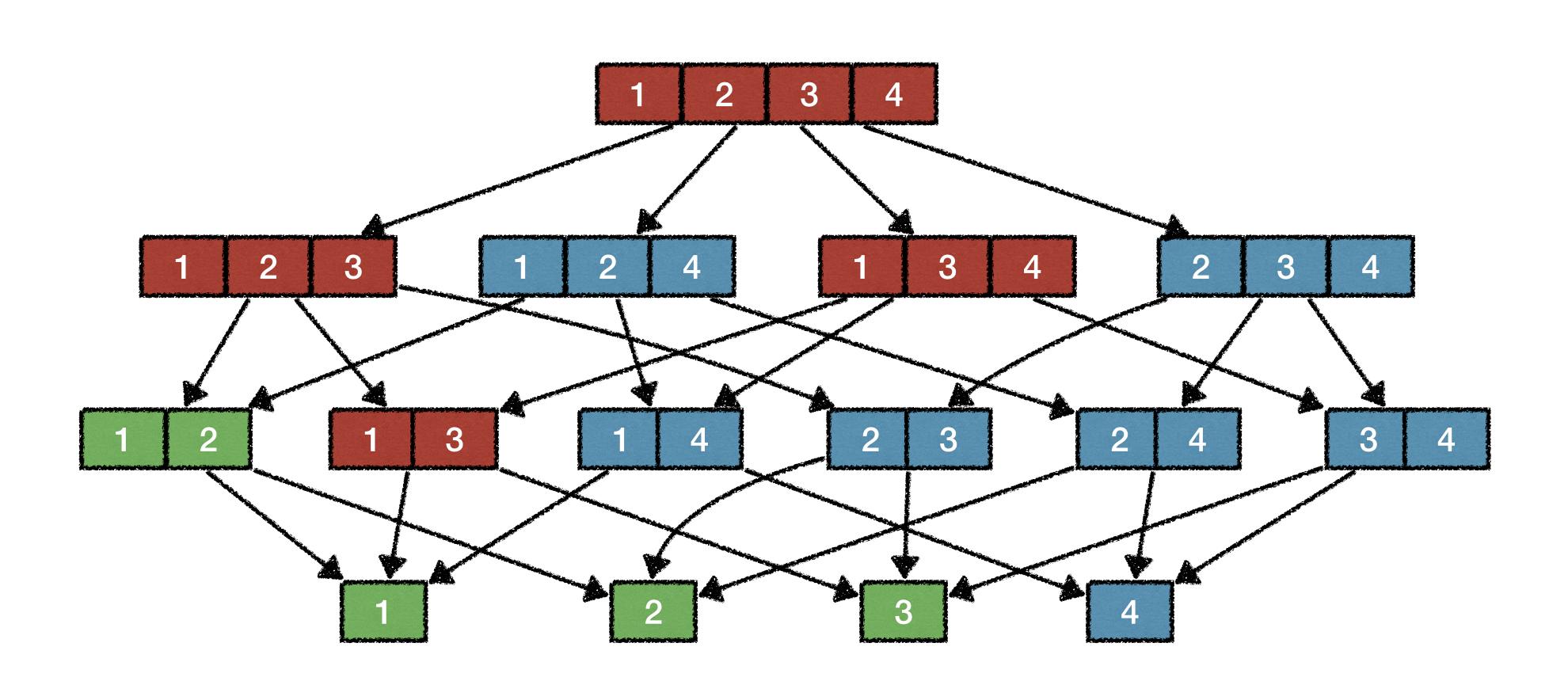
### 组合测试故障定位经典框架



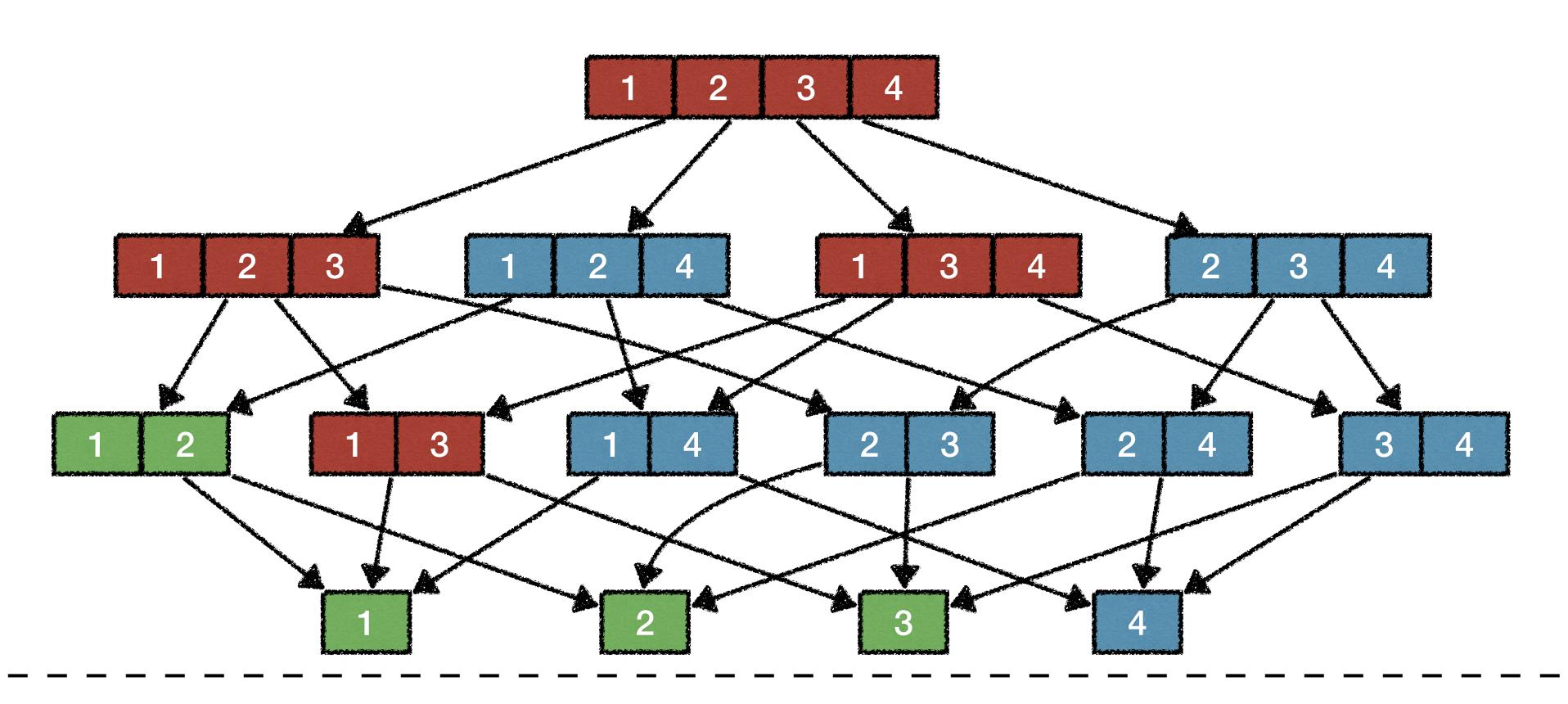








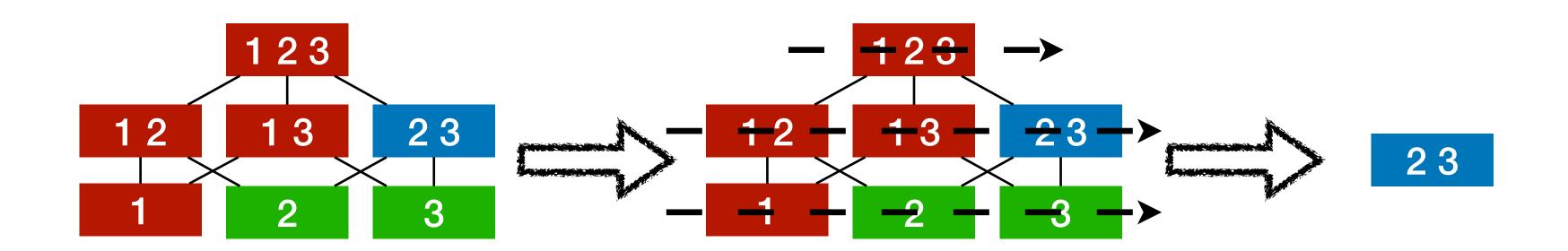
### 无法被确定的元组一待定元组





待定元组(pending schema)是已有方法难以获得完整(Complete)结果的根本原因。

- 一个简单的想法:
  - 给出元组树,然后不断的扫描和确定每一个元组



代价是空间复杂度 $O(2^n)$ ,时间复杂度也是 $O(2^n)$ 

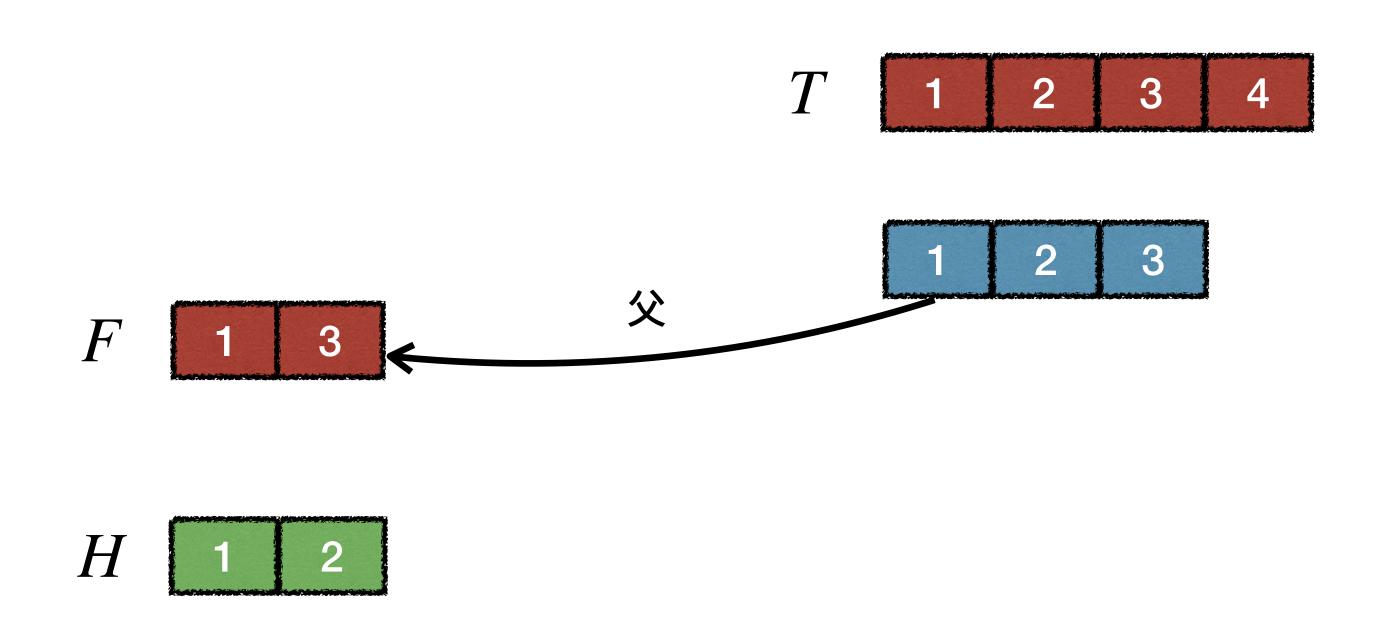
- 待定元组的两个条件:
  - 1. 不能是已有任何故障元组的父元组
  - 2. 不能是已有任何健康元组的 子元组

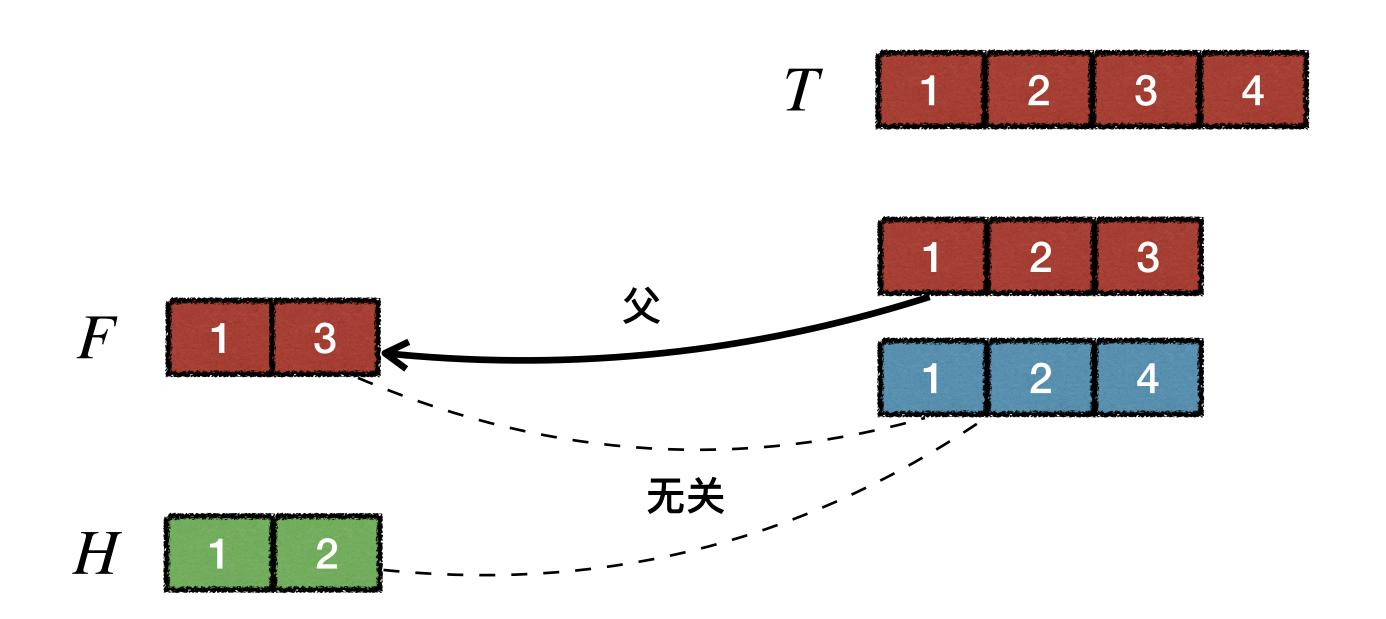
- 输入: 已有故障元组集F,已有健康元组集H,一条错误的测试用例T
- 过程: 枚举T中所有的元组
  - 检查其是否是任何一个故障元组的父元组。
  - 检查其是否是任何一个健康元组的子元组。
  - 如果都不满足,其为待定元组。

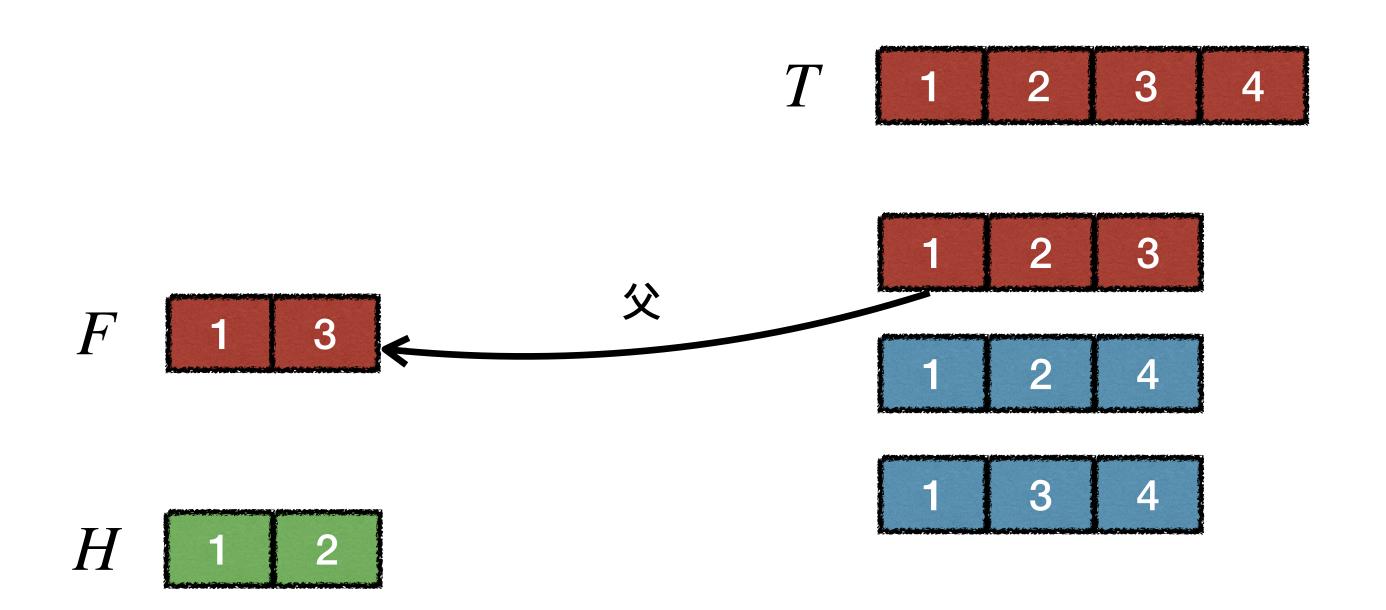
T 1 2 3 4

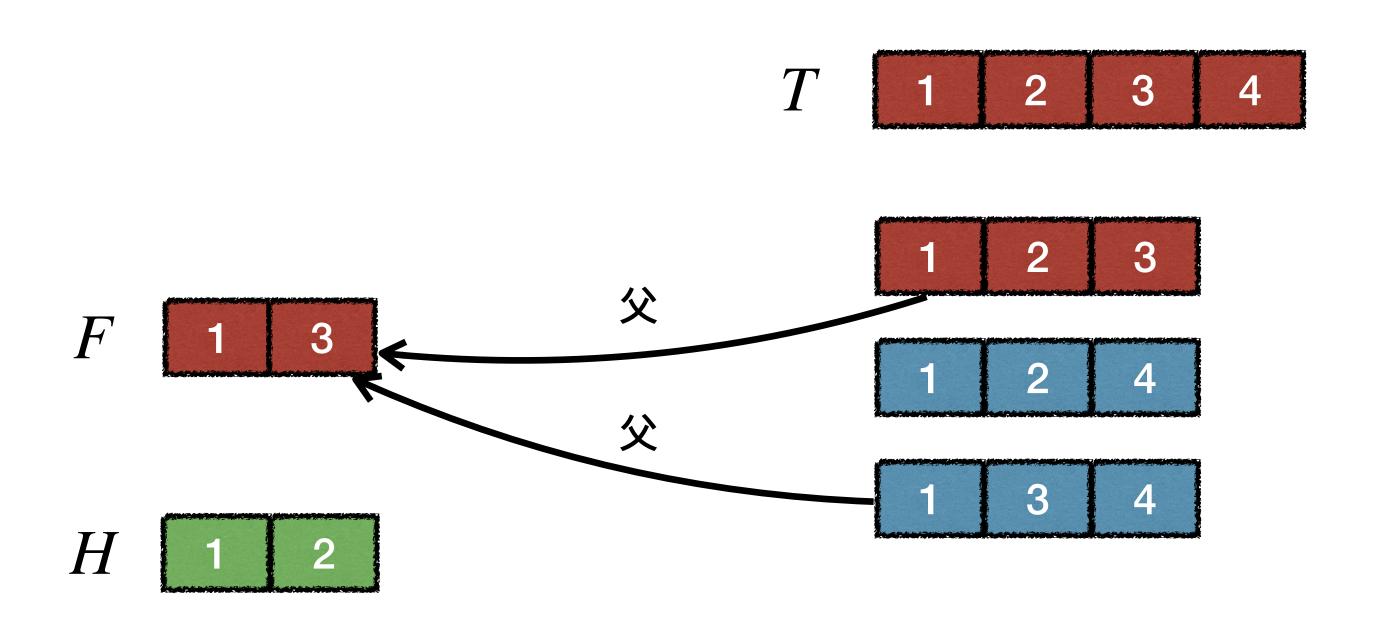
F 1 3

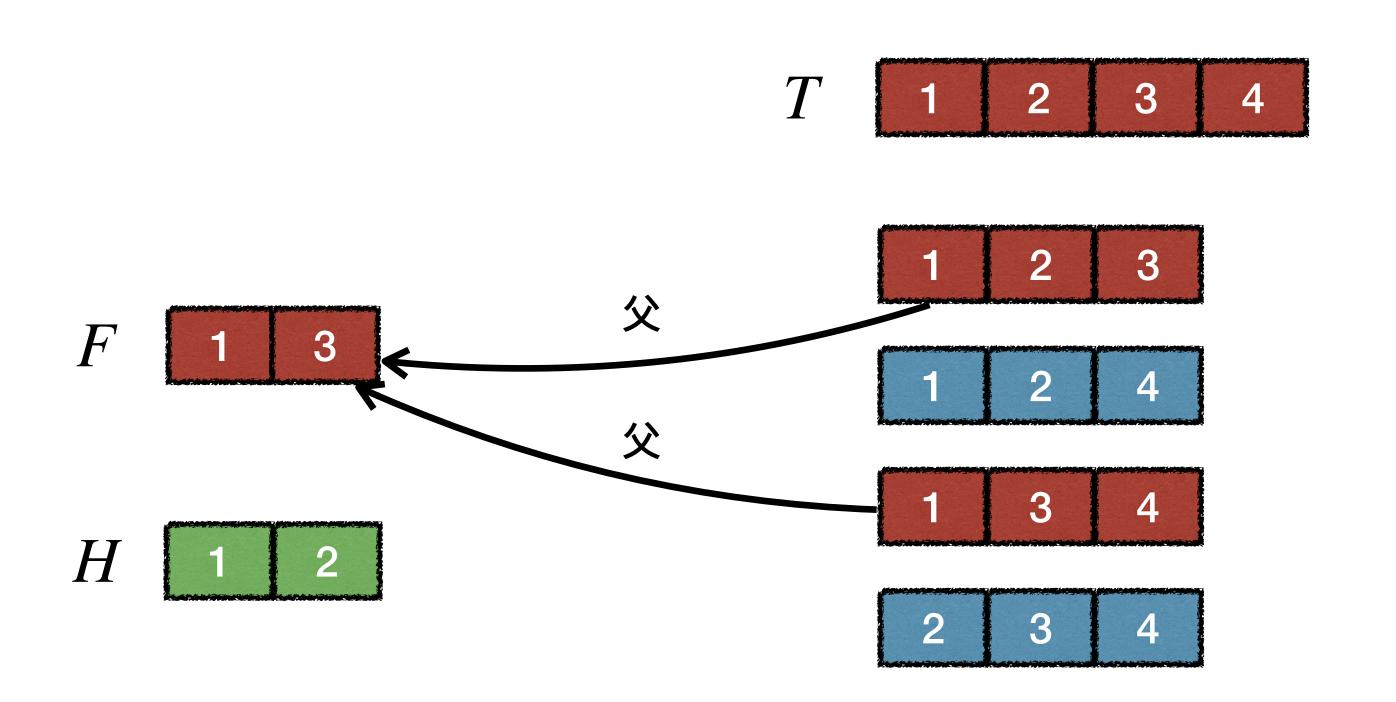
H 1 2

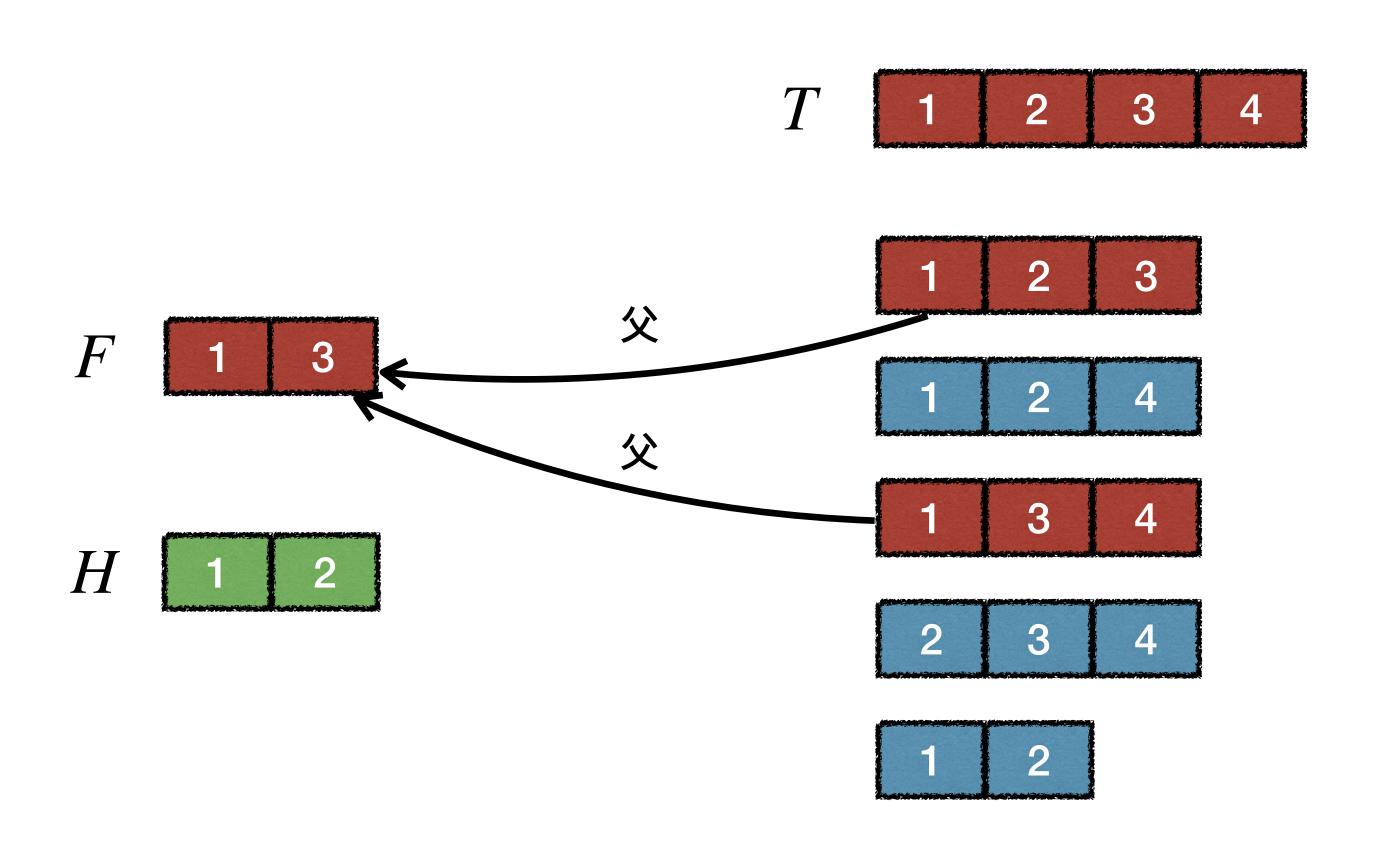


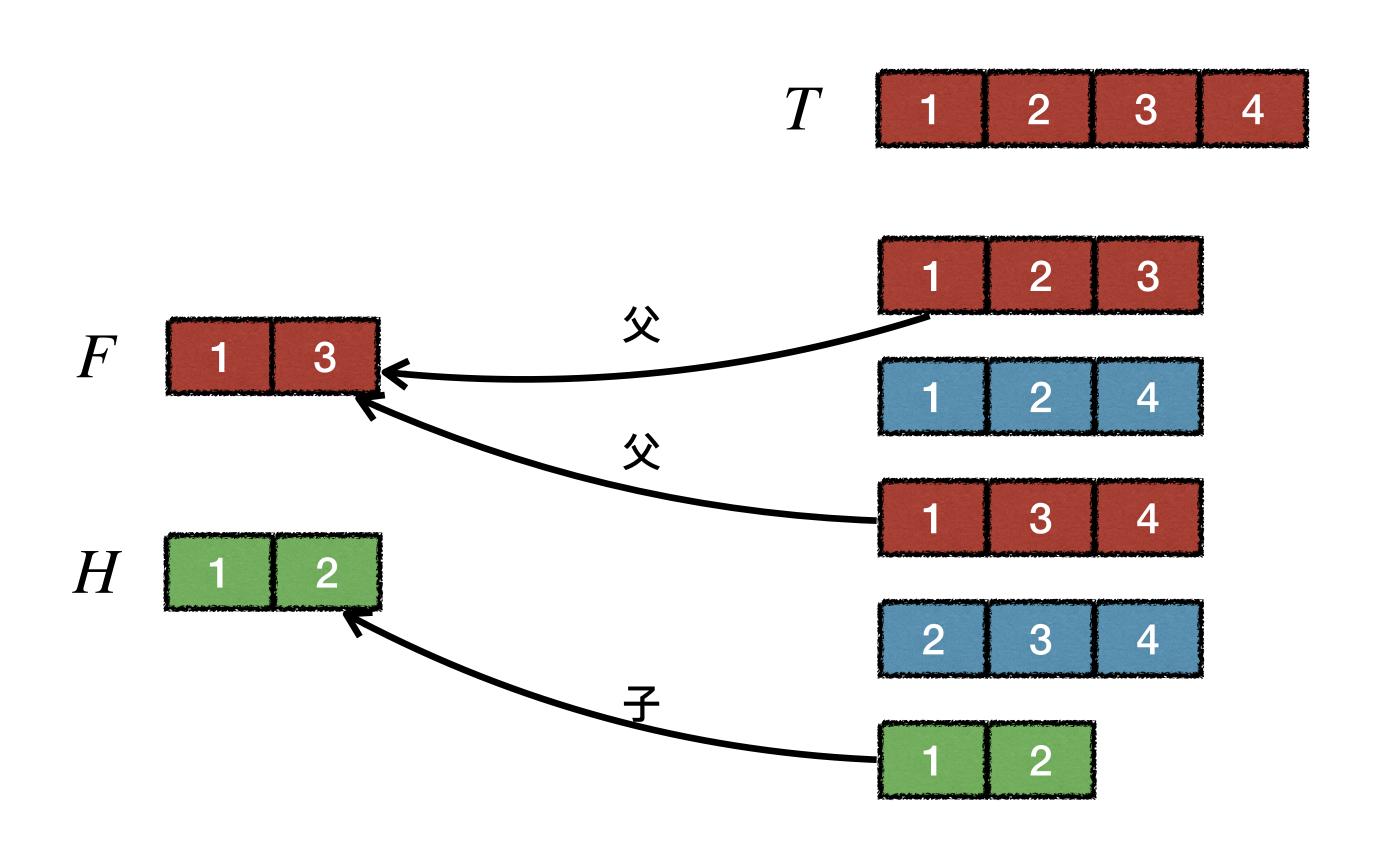


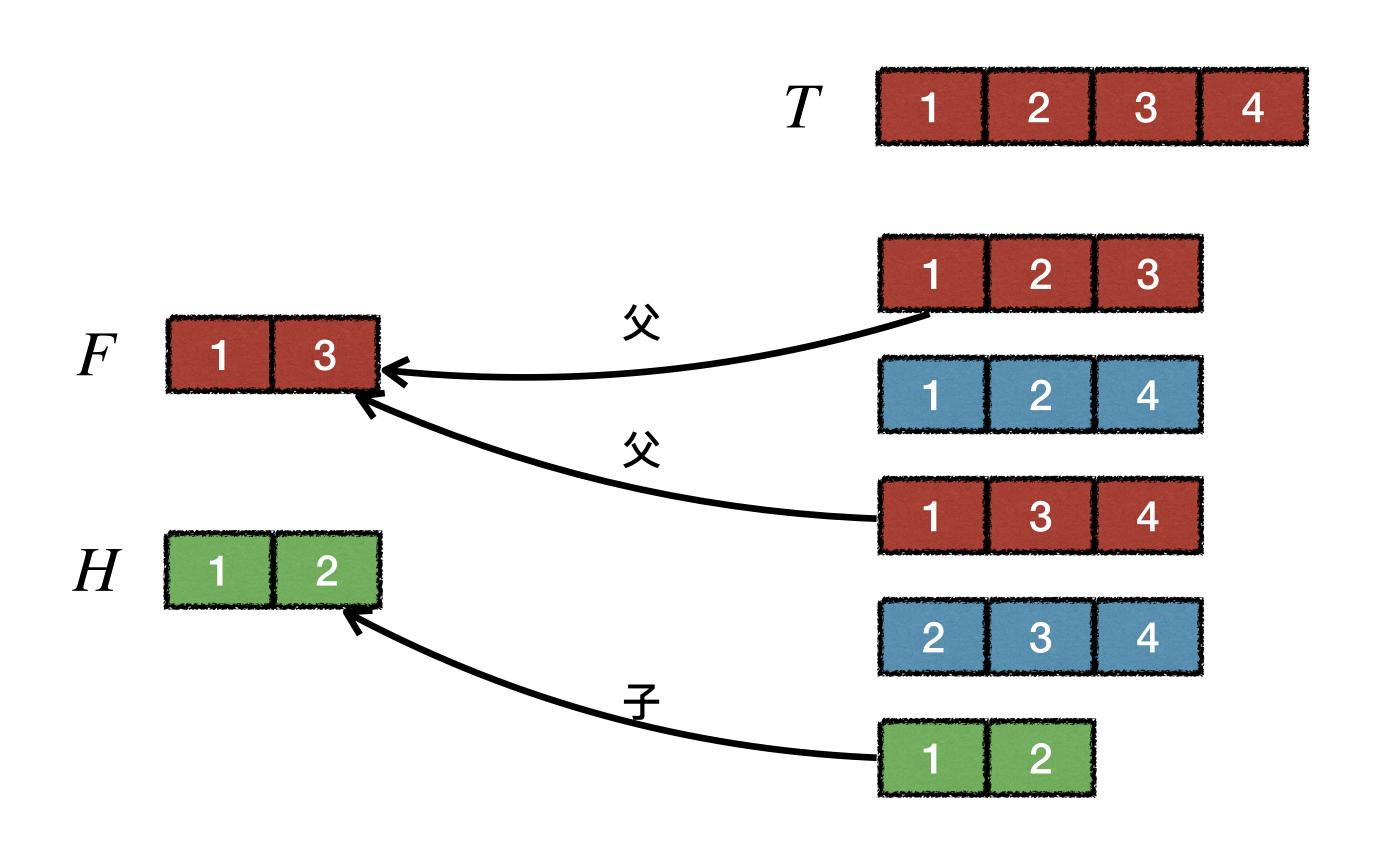








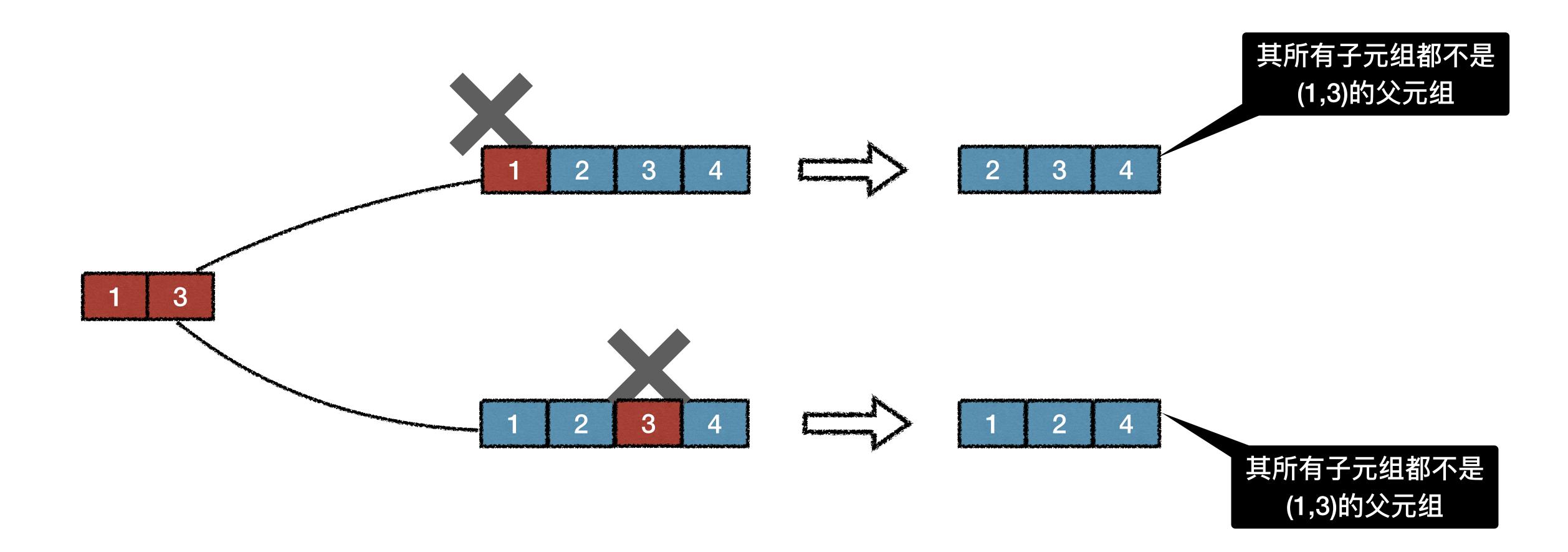




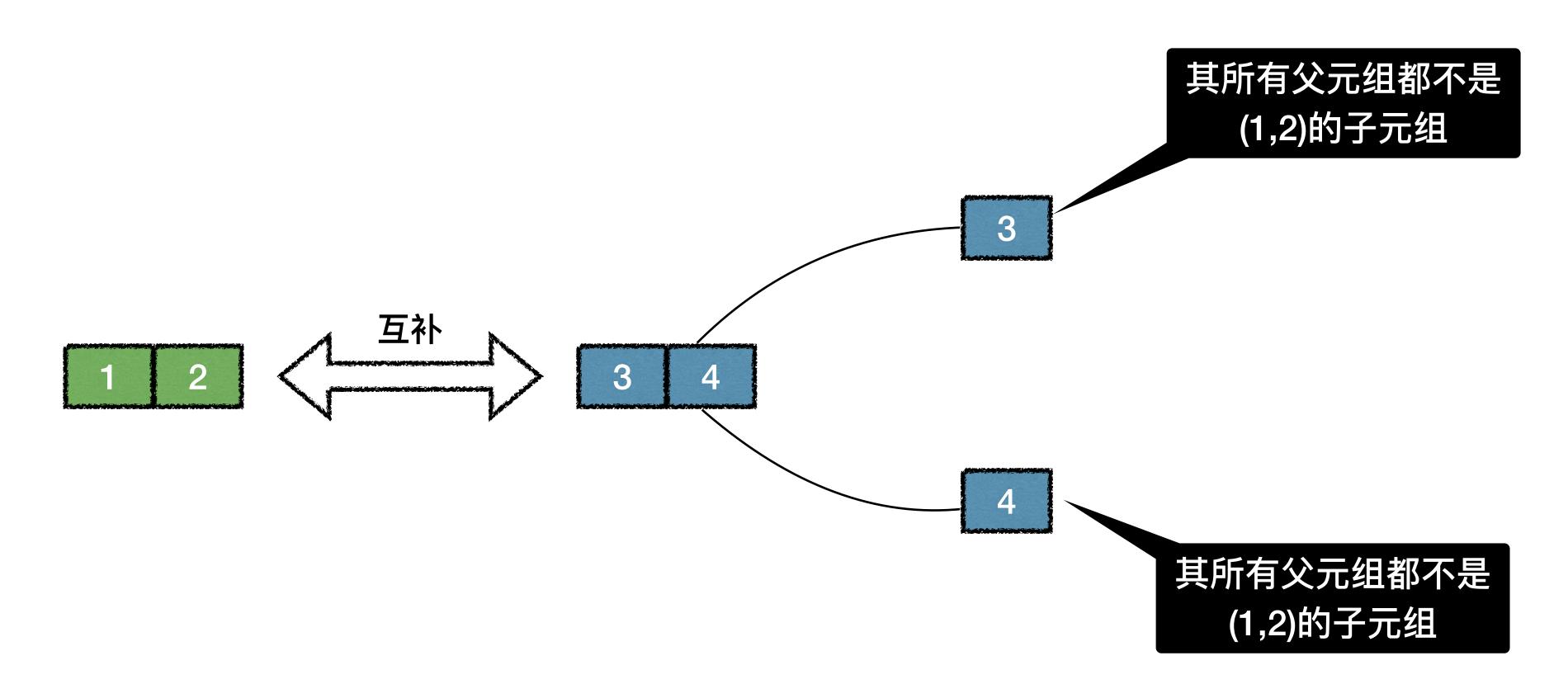
代价是时间复杂度是 $O(2^n)$ 

- 之前方法复杂度大的原因:两个性质是负面的(negative)。
  - 1. 不能是已有任何故障元组的父元组
  - 2. 不能是已有任何健康元组的子元组

● 不是某故障元组的父元组 ← 至少剔除其中一个元素即可



● 不是某健康元组的子元组 ← 至少包含一个其没有的元素即可



● 不是某故障元组的父元组 ← 至少剔除其中一个元素即可

同时满足

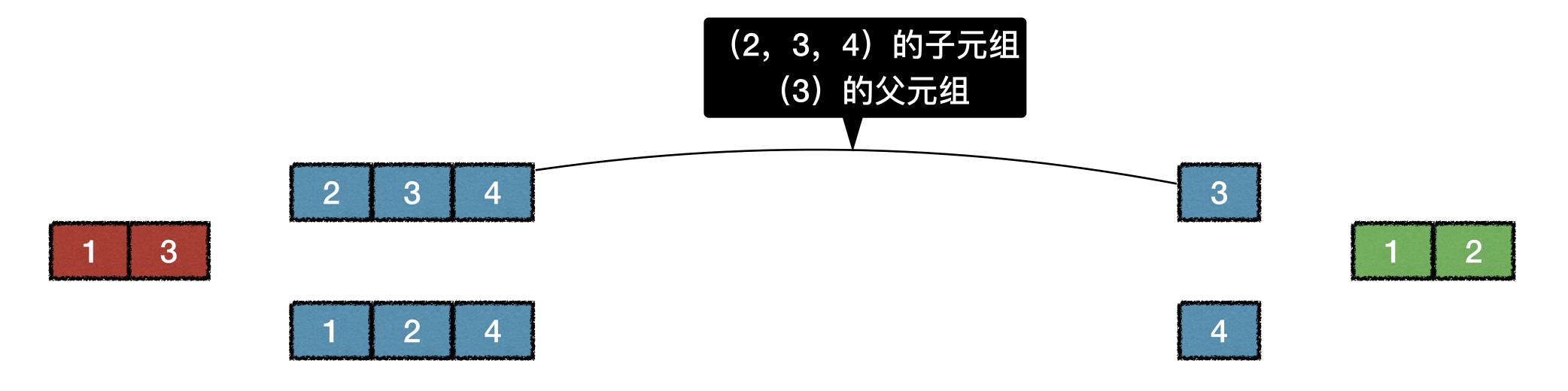
● 不是某健康元组的子元组 ← 至少包含一个其没有的元素即可

2 3 4

● 不是某故障元组的父元组 ← 至少剔除其中一个元素即可

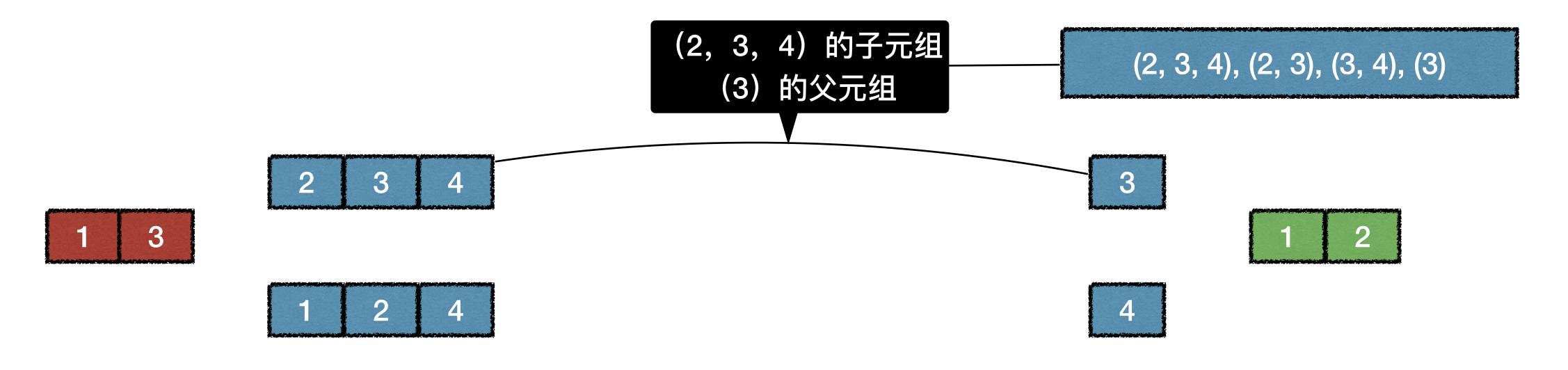
同时满足

● 不是某健康元组的子元组 ← 至少包含一个其没有的元素即可



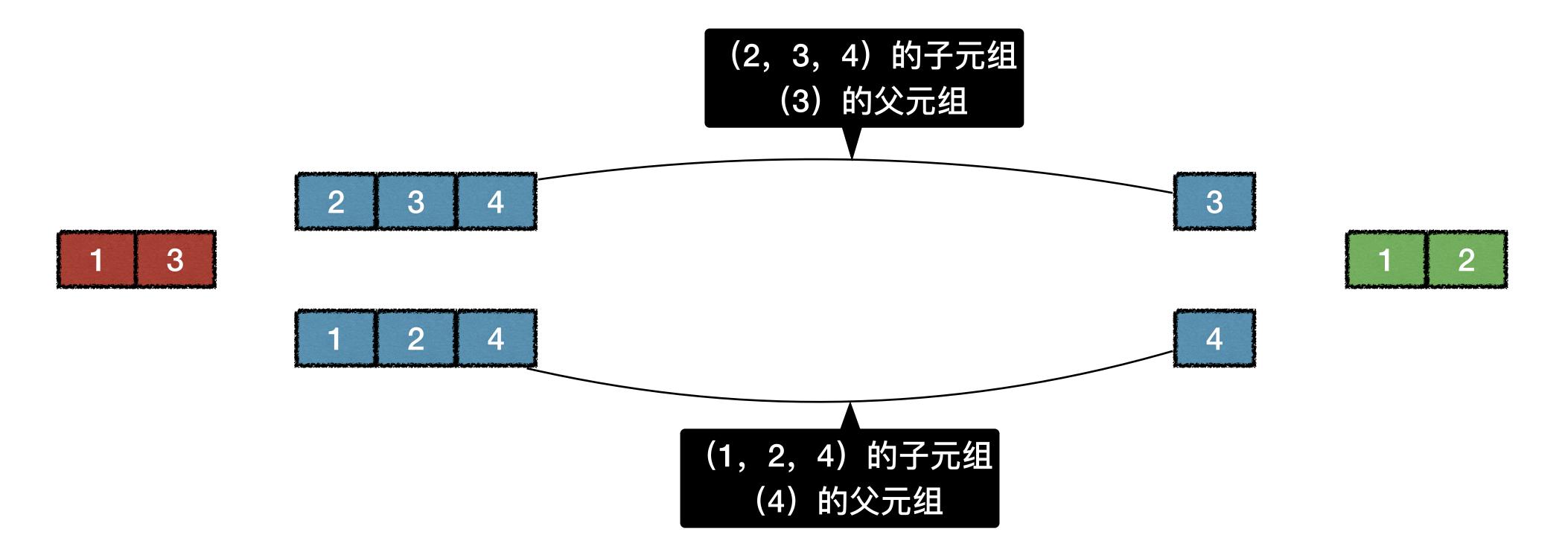
● 不是某故障元组的父元组←→至少剔除其中一个元素即可

同时满足



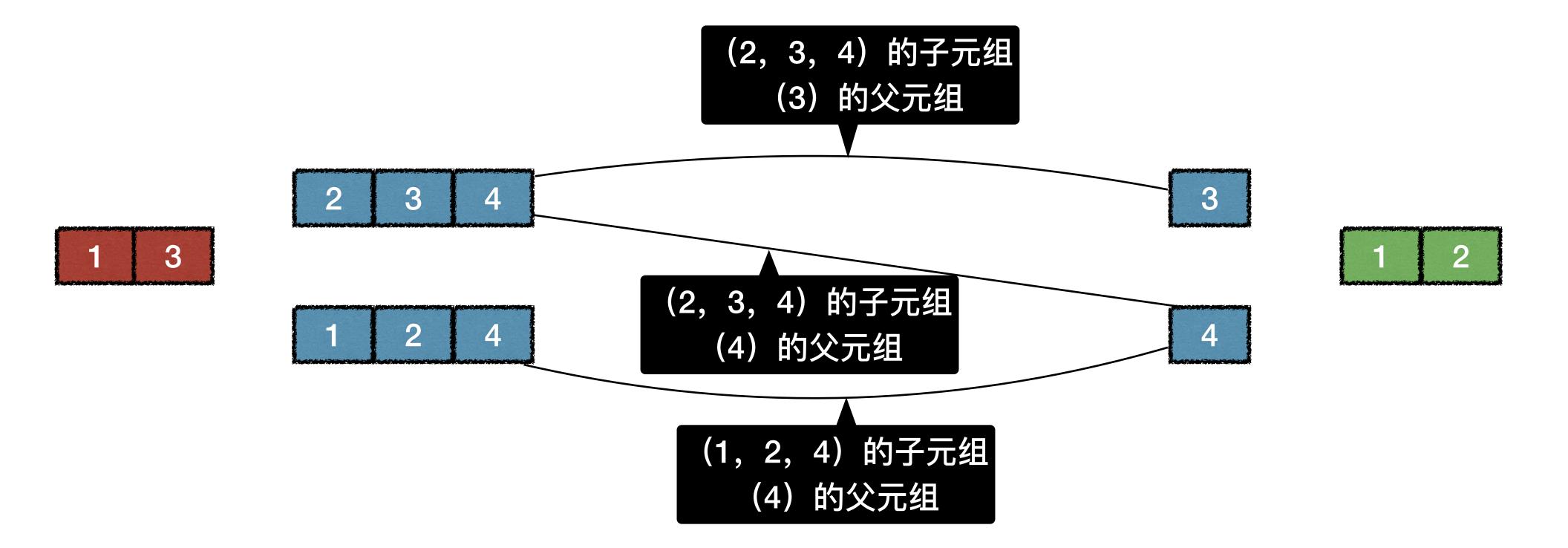
● 不是某故障元组的父元组 ← 至少剔除其中一个元素即可

同时满足



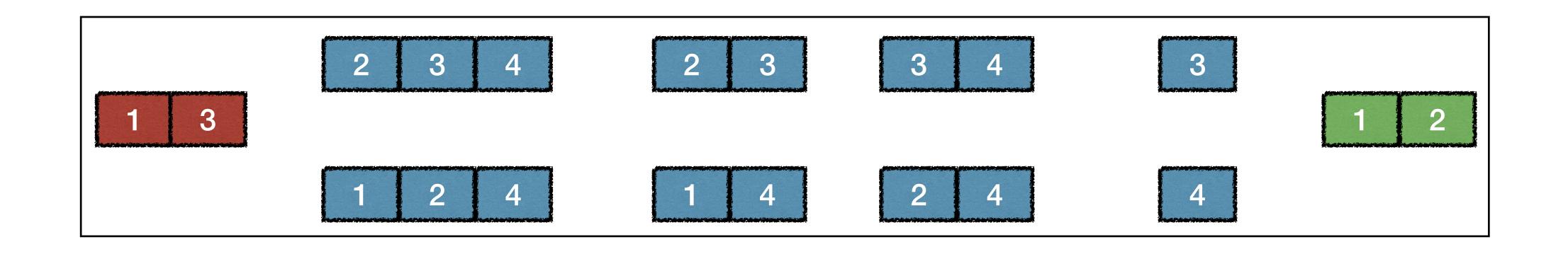
● 不是某故障元组的父元组 ← 至少剔除其中一个元素即可

同时满足

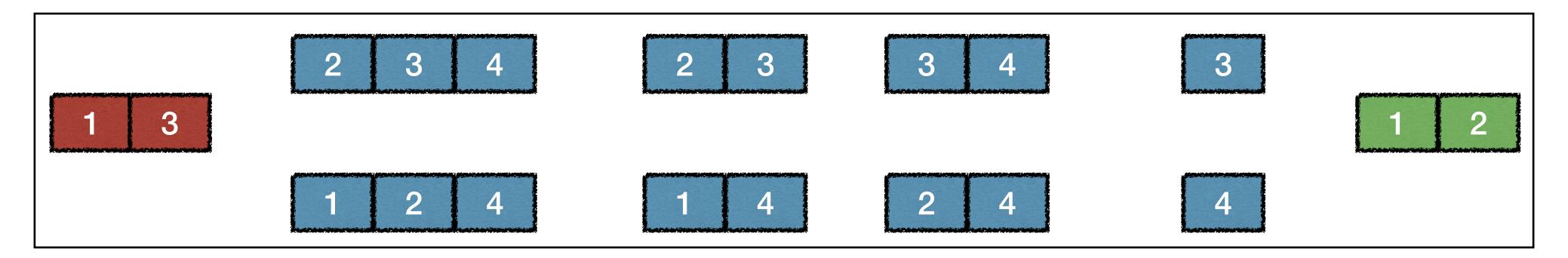


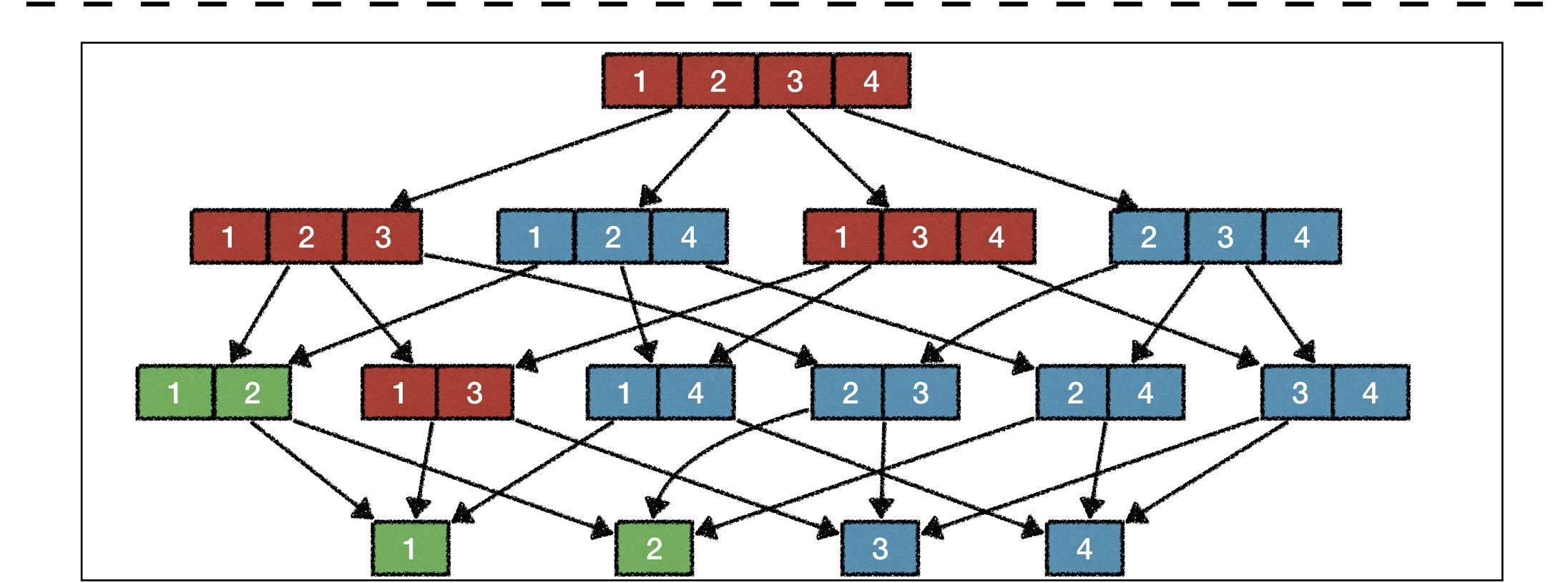
● 不是某故障元组的父元组 ← 至少剔除其中一个元素即可

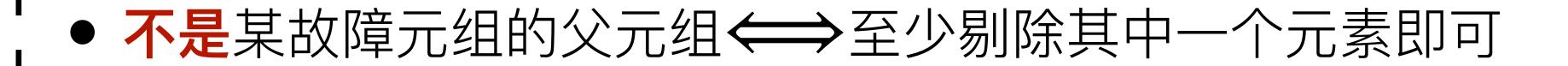
同时满足



# 两者结果相等







1 2

● 不是某健康元组的子元组 ← 至少包含一个其没有的元素即可

• 不是多个故障元组的父元组?

1 3

2 4

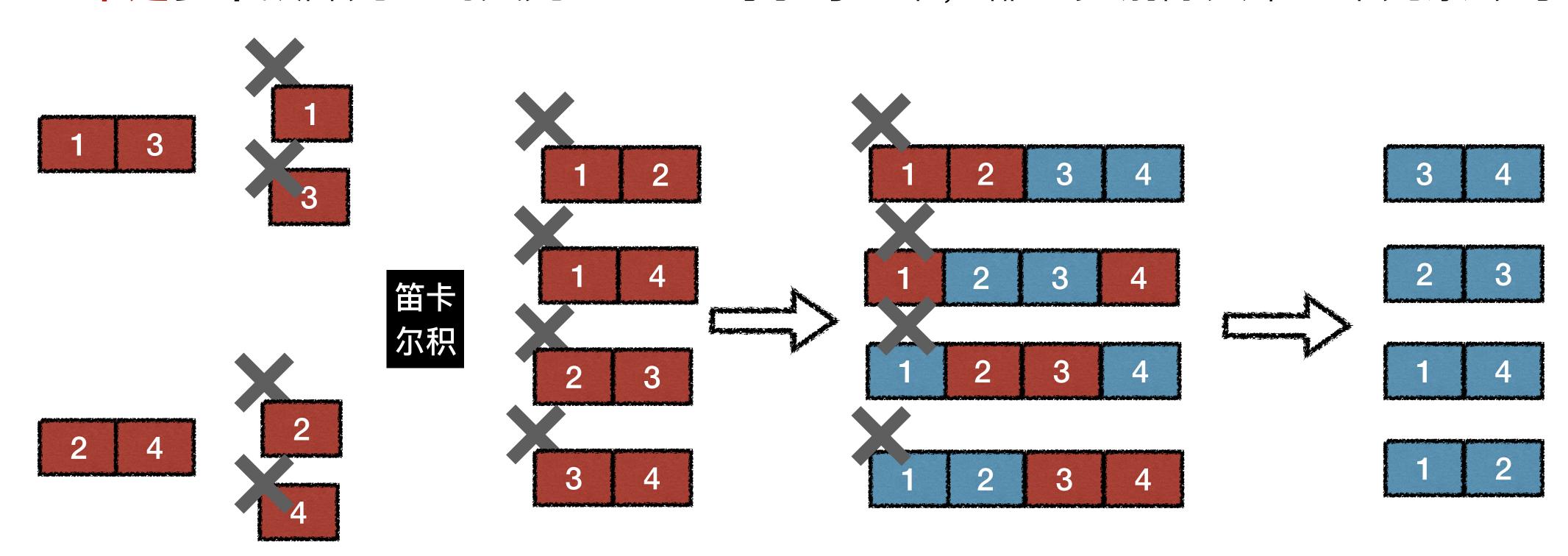
1 2

3

• 不是多个健康元组的子元组?

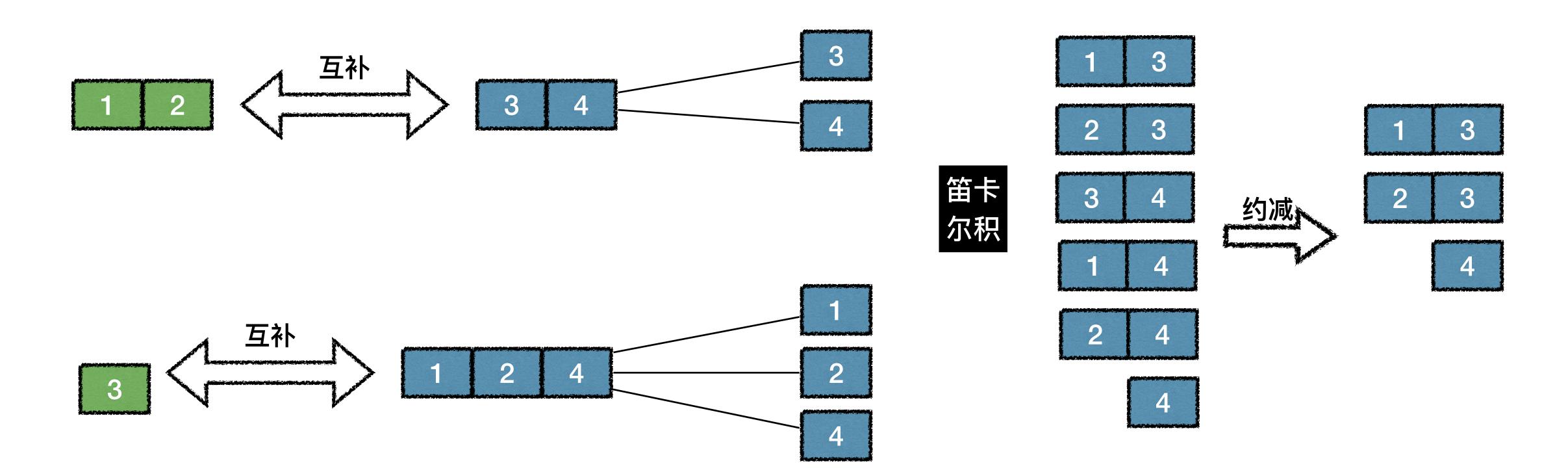
- 拓展到多个故障元组,多个健康元组
  - **不是多个**故障元组的父元组<del>←→</del>对于每一个,都至少剔除其中一个元素即可
    - 一>对每一个故障元组都至少选一个元素,进行合并剔除
    - 一>所有故障元组元素的笛卡尔积

- 拓展到多个故障元组,多个健康元组
  - **不是多个**故障元组的父元组<del>(→</del>对于每一个,都至少剔除其中一个元素即可



- 拓展到多个故障元组,多个健康元组
  - **不是多个**健康元组的子元组<del>(→</del>对于每一个,都至少包含一个其没有的元素
    - 一>对每一个健康元组,都至少选一个其不包含的元素,进行合并。
    - 一>所有健康元组的补集的元素的笛卡尔积

- 拓展到多个故障元组,多个健康元组
  - **不是多个**健康元组的子元组<del>(→</del>对于每一个,都至少包含一个其没有的元素



- 关键转换
  - **不是多个**故障元组的父元组<del>(→</del>对于每一个,都至少剔除其中一个元素即可
  - **不是多个**健康元组的子元组<del>(→</del>对于每一个,都至少包含一个其没有的元素
- 计算复杂度  $O(2^n \times n \times c)$  降到 $O(n^{1+c})$  , 其中n是测试用例的元素个数,而c是一个较小的数,与n无关

Subject	n	$ \hat{\mathcal{U}}(T_{fail}) $	$ T_{pass} $	Worst Alg#3 (Time under 4Ghz)	Best Alg#2 (Time under 4Ghz)
Totem-2.17.5	28	1	$\Theta(log_228)$	$28^{1+1+log_228} \approx 7.1 \times 10^9 \ (1.8 \ s)$	$2^{28} \times 28 \times 2 \approx 1.5 \times 10^{10}$ (3.8 s)
bash-4.2	76	1	$\Theta(log_276)$	$76^{1+1+log_276} \approx 3.3 \times 10^{15} \ (9.4 \ days)$	$2^{76} \times 76 \times 2 \approx 1.1 \times 10^{25} \text{ (9} \times 10^7 \text{ years)}$
lua(one commit)	60	1	$\Theta(log_260)$	$60^{1+1+log_260} \approx 1.1 \times 10^{14} \ (8.0 \ hours)$	$2^{60} \times 60 \times 2 \approx 1.4 \times 10^{20} \text{ (1096 years)}$
vim (one commit)	56	1	$\Theta(log_256)$	$56^{1+1+log_256} \approx 4.5 \times 10^{13} \ (3.1 \ hours)$	$2^{56} \times 56 \times 2 \approx 8.1 \times 10^{18} $ (63.9 years)
libxml2-2.9.0	66	1	$\Theta(log_266)$	$66^{1+1+log_266} \approx 4.3 \times 10^{14} (1.3 \ days)$	$2^{66} \times 66 \times 2 \approx 9.7 \times 10^{21} \ (7.7 \times 10^4 \ years)$
libpng-1.6.0	87	1	$\Theta(log_287)$	$87^{1+1+log_287} \approx 2.4 \times 10^{16} (68.7 \ days)$	$2^{87} \times 87 \times 2 \approx 2.7 \times 10^{28} \text{ (2.1} \times 10^{11} \text{ years)}$
gnuplot-4.6.1	45	2	$\Theta(log_245)$	$45^{1+2+log_245} \approx 1.1 \times 10^{14} \ (7.6 \ hours)$	$2^{45} \times 45 \times 2 \approx 3.2 \times 10^{15}$ (9.2 days)
gnome-vfs-2.13.92	26	1	$\Theta(log_226)$	$26^{1+1+log_226} \approx 3.0 \times 10^9 \ (0.8 \ s)$	$2^{26} \times 26 \times 2 \approx 3.4 \times 10^9 \ (0.9 \ s)$

### Pending Tse 2021

### 组合测试中的待定模式理论

Xintao Niu, Huayao Wu, Changhai Nie, Yu Lei, and Xiaoyin Wang. A theory of pending schemas in combinatorial testing. IEEE Transactions on Software Engineering (TSE), in press, available online in 2021

IEEE TRANSACTIONS ON SOFTWARE ENGINEERING

### A Theory of Pending Schemas in Combinatorial Testing

Xintao Niu<sup>®</sup>, *Member, IEEE*, Huayao Wu<sup>®</sup>, *Member, IEEE*, Changhai Nie, *Member, IEEE*, Yu Lei<sup>®</sup>, *Member, IEEE*, and Xiaoyin Wang<sup>®</sup>, *Member, IEEE* 

Abstract—Combinatorial Testing (CT) is an effective testing technique for detecting failures which are triggered by the interactions of various factors that influence the behaviour of a system. Although many studies in CT have designed elaborate test suites (called covering arrays) to systemically check each possible factor interaction, they provide weak support to locate the concrete failureinducing interactions, i.e., the Minimal Failure-causing Schemas (MFS). To this end, a variety of MFS identification approaches have been proposed. However, as this study reveals, these approaches suffer from various issues such as cannot identify multiple overlapping MFSs, cannot handle MFSs with high degrees, cannot be applied to systems with large number of parameters, etc. These issues are essentially caused by the exponential computing complexity of checking every interaction in the test cases. Therefore, they can only focus on a subset of all the possible interactions, resulting in many interactions unnoticed. Ignoring these unnoticed interactions could potentially cause failures that have never been systematically checked. Hence, it is beneficial for MFS identification approaches to identify these interactions. In order to account for these unnoticed interactions in CT, this study introduces the notion of pending schema, based on which a theoretical framework of CT schemas is established. In particular, we formally define the determinability of a schema in CT with respect to given information; as such, the yet-to-be determined schemas are exactly the pending schemas. The relationships between the different schemas (faulty, healthy, and pending) and test cases are also theoretically analyzed. Based on which, we further propose three formulas, along with three corresponding algorithms, for the identification of the pending schemas in failing test cases, and formally prove their correctness. As a result, we reduce the complexity of obtaining pending schemas with respect to the number of factors that may have influences on the software.

Index Terms—Pending schema, minimal failure-causing schema, combinatorial testing, software testing

### 1 Introduction

THE behavior of modern software is affected by many ▲ factors, such as input parameters, configuration options, and communication events. To test such a software system is challenging, as, in theory, we should test all the possible interactions of these factors to ensure the correctness of the System Under Test (SUT) [1], [2]. Since the number of interactions to be checked increases exponentially with respect to the number of factors, exhaustive testing is not feasible.

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Manuscript received 19 May 2020; revised 23 Aug. 2021; accepted 16 Sept. 2021. Date of publication 0 . 0000; date of current version 0 . 0000.

This work was supported in part by the National Key Research and Development Program of China under Grant 2018YFB1003800, in part by the National Natural Science Foundation of China under Grants 61902174 and 62072226, in part by the Natural Science Foundation of Jiangsu Province under Grant BK20190291, and in part by Information Technology Laboratory at National Institute of Standards and Technology under Grant 70NANB18H207.

(Corresponding author: Xintao Niu.) Recommended for acceptance by K. Sen. Divital Object Identifier no. 10.1109/TSE.2021.3113920 Combinatorial Testing (CT) is a promising solution to handle the combinatorial explosion problem [3], [4]. Instead of testing all the possible interactions in a system, it focuses on checking those interactions with the number of involved factors no more than a predefined constant. Many studies in CT focus on designing an elaborate test suite (called covering array) to reveal such failures. Although covering arrays are effective and efficient as test suites, they provide weak support to distinguish the failure-inducing interactions, i.e., Minimal Failure-causing Schemas (MFS), from other interactions (schemas) [5], [6].

As an example [7], Table 1 presents a pair-wise covering array for testing an MS-Word application in which we want to examine various pair-wise interactions of options for 'Highlight', 'Status Bar', 'Bookmarks' and 'Smart tags'. Assume the last test case fails. We can derive six pair-wise suspicious schemas that may be responsible for this failure. They are respectively (Highlight: On, Status Bar: Off), (Highlight: On, Bookmarks: On), (Highlight: On, Smart tags: On), (Status Bar: Off, Bookmarks: On), (Status Bar: Off, Smart tags: On), and (Bookmarks: On, Smart tags: On). Without additional information, it is difficult to figure out the specific failure-causing schemas in this suspicious set. In fact, considering that the schemas of different sizes could also be MFS, e.g., (Highlight: On, Status Bar: Off, Smart tags: On), the problem becomes more complicated. We listed all the schemas contained in this test case at the left table of Fig. 1, which contains 15 schemas (the dash '-' indicates the corresponding factor is not involved in the

### Reviewer: 2

Public Comments (these will be made available to the author)

The combinatorial explosion is one of the challenges in identifying failure-inducing interactions, i.e., Minimal f causing schemes (MFS). Despite the existing techniques to determine MFS in a failing test case, these techni fell short in determining pending schemas, i.e., schemas that, yet, cannot be labeled as faulty or not. In this the authors proposed a new approach to identifying the pending schemas in one test case.

To begin with, this is a fascinating study. I praise the authors for their contribution to the community. They w to convey a strong motivation to define the term pending schema formally. Additionally, the authors provided algorithms that rely on theorems to identify the pending schemas. The authors demonstrated how their algor could reduce the computational complexing of obtaining pending schemas; thus, reducing the combinatorial associated with the number of factors.

I can divide the study highlights into three categories. The first one is the study motivation. I believe the aut an excellent job of motivating the study. The importance and challenges in identifying pending schemes are of formalization of pending schemas is the second high point in the study. They defined characterize and identify pending schemas. Of course, this level of formalization is wh work like that. However, the authors presented the formalization for each concept an and didactic way. The same incremental strategy was used to present the theorems at the authors for their contribution to the community. algorithms, which make the understanding of these sections easier than they normal discussion of the impacts of constraints, which provides a more realistic scope of the approach will be applied.

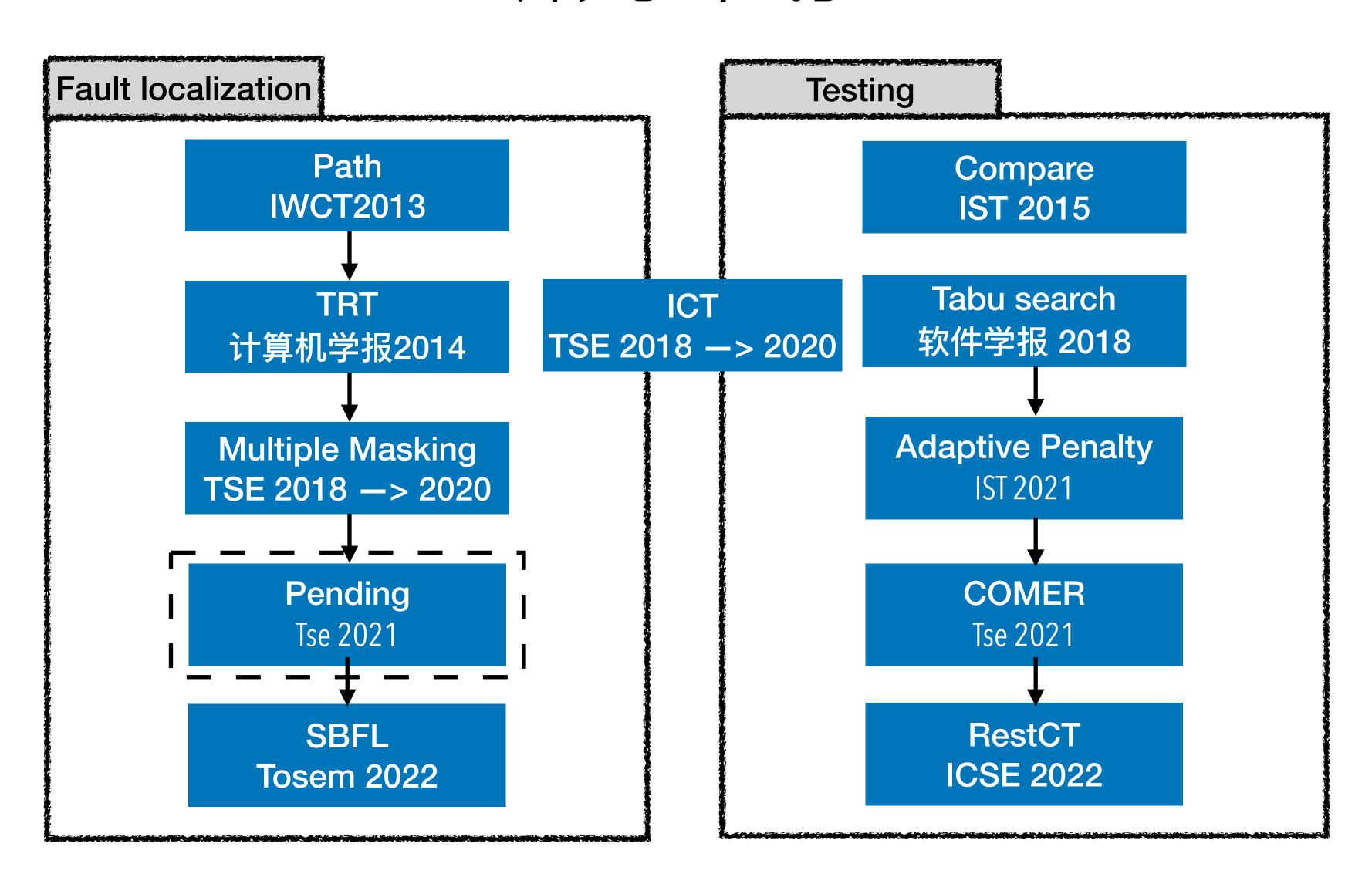
To begin with, this is a **fascinating** study. I **praise** 

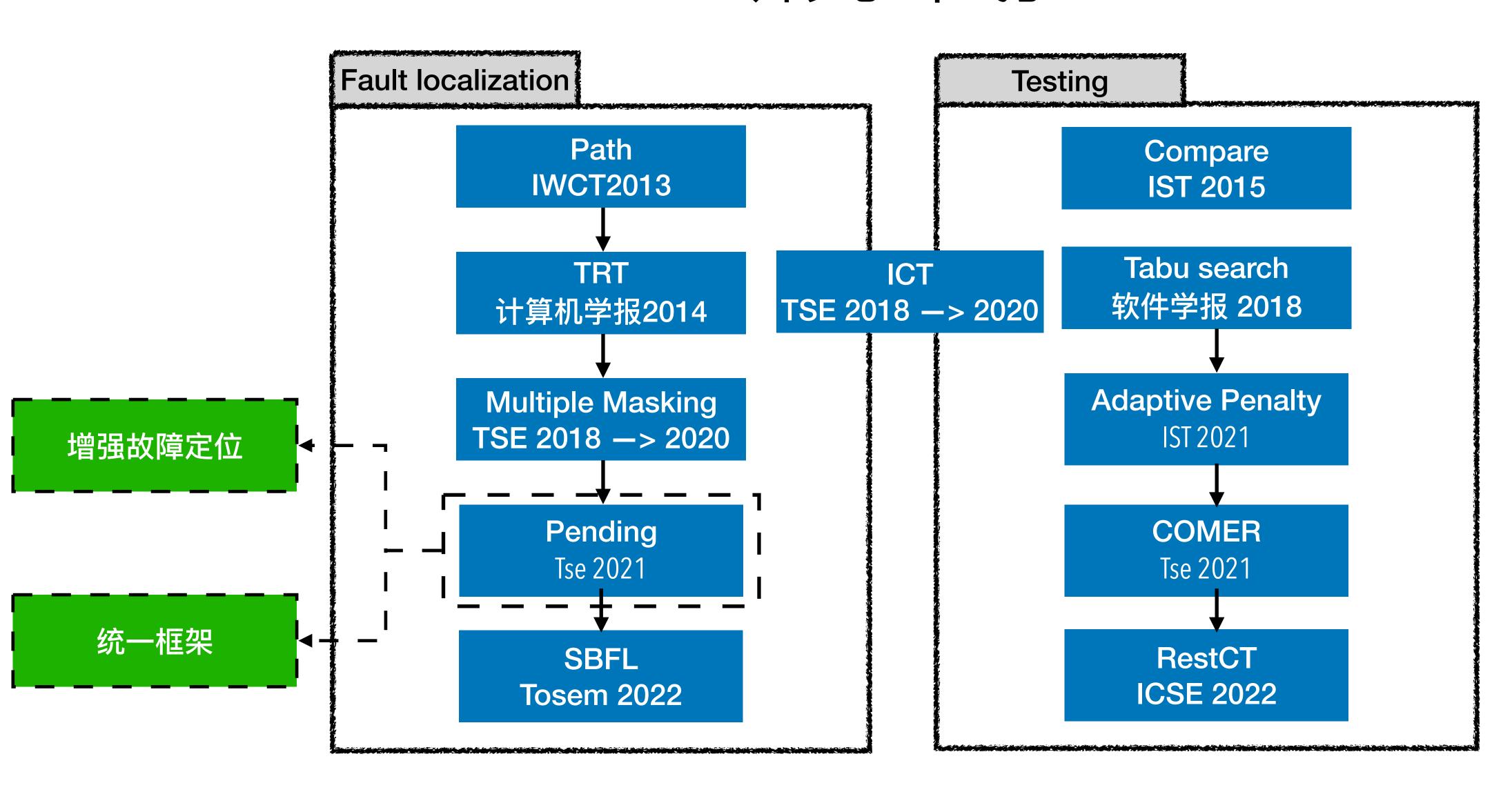
The addressed problem is indeed significant, and the provided analysis gives useful insights on the problem of identifying pending schemas.

### **EVALUATION**

The paper is well written, easy to understand, and well structured.

The addressed problem is indeed significant, and the provided analysis gives useful insights on the problem of identifying pending schemas.

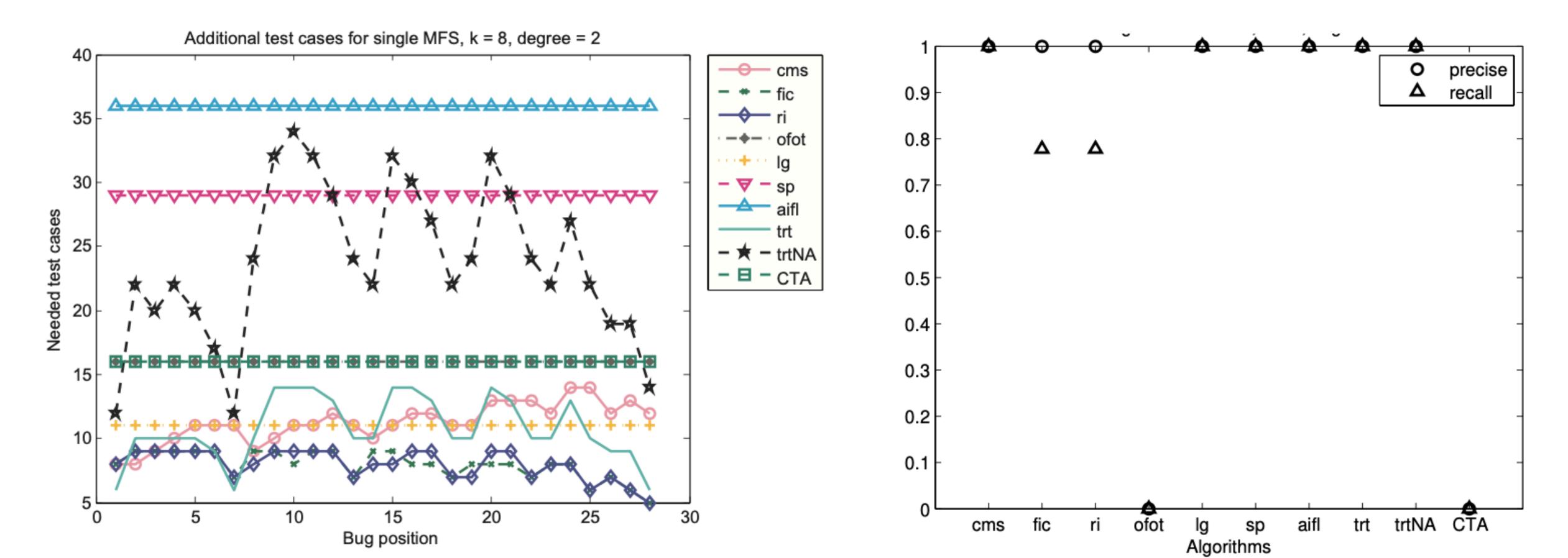




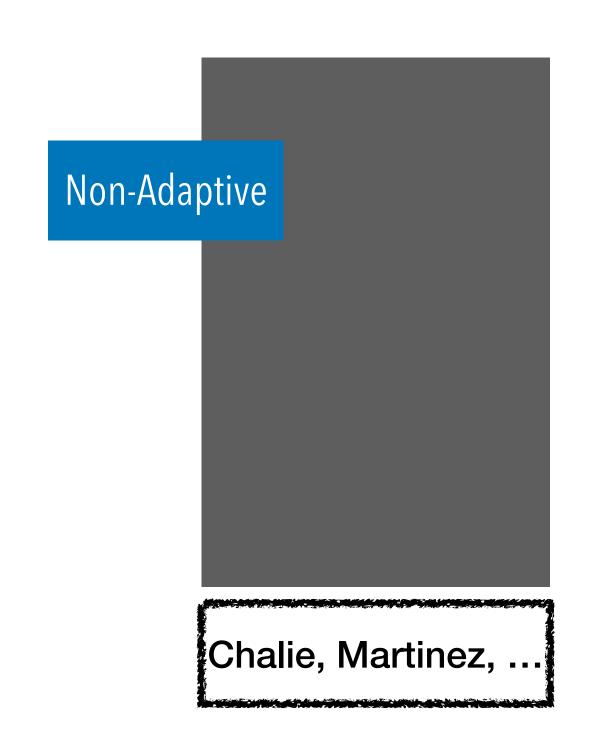
● 以待定元组(pending schema)为导向的组合测试故障定位方法

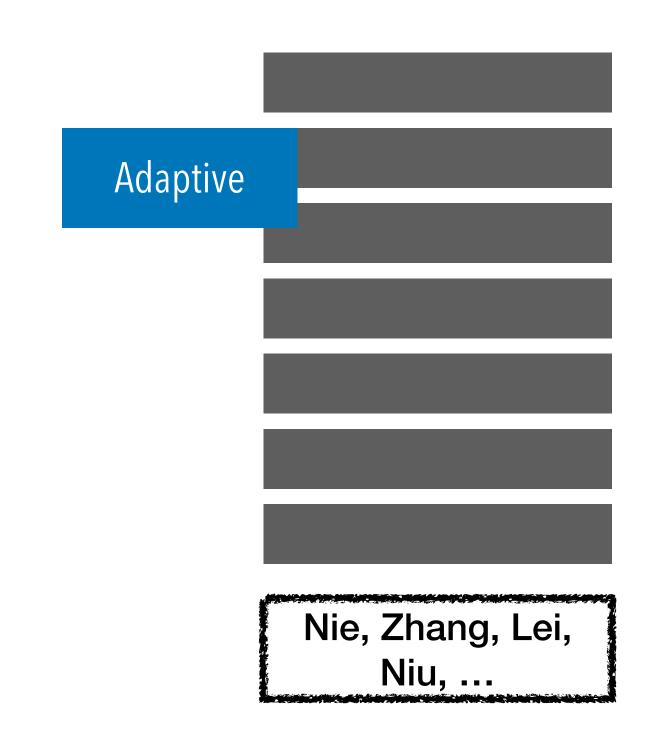
- 从传统的得到一个故障元组为终止目标->待定元组个数为0的终止目标 为空集 停止 获得待定元组 部分故障定位

● 以待定元组为导向的组合测试故障定位方法—初步结果

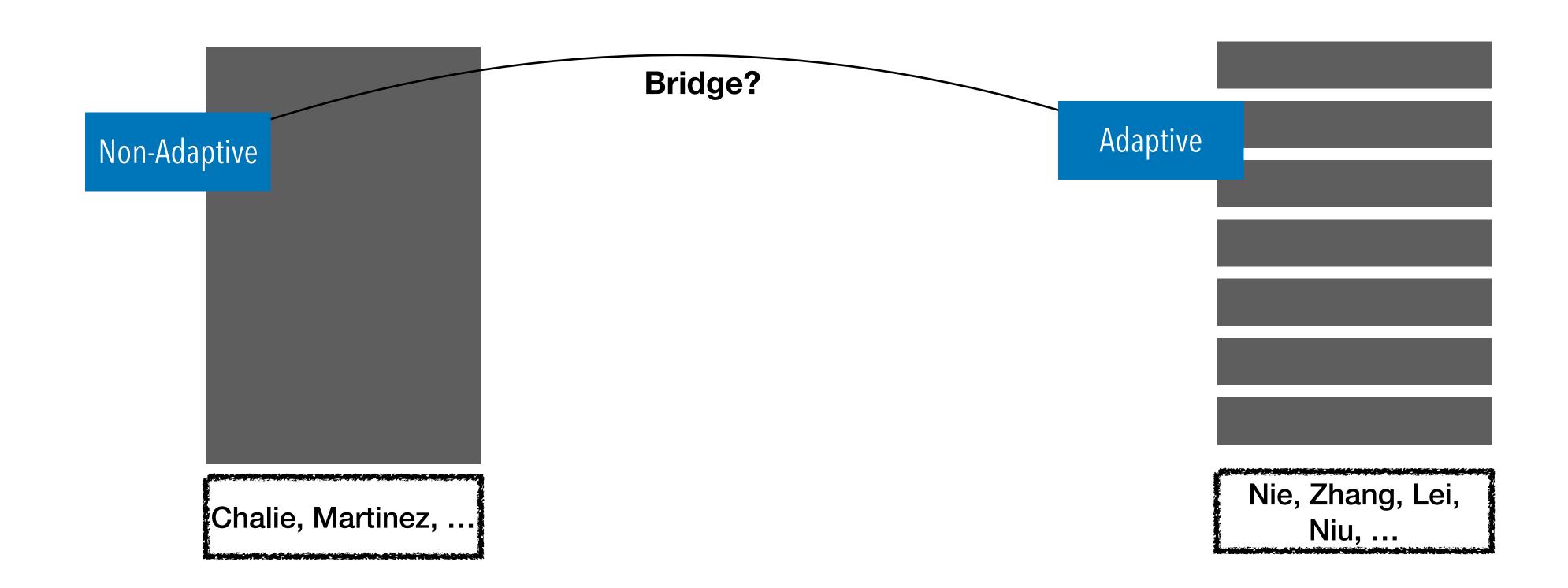


• 构建一个统一的故障定位理论和框架

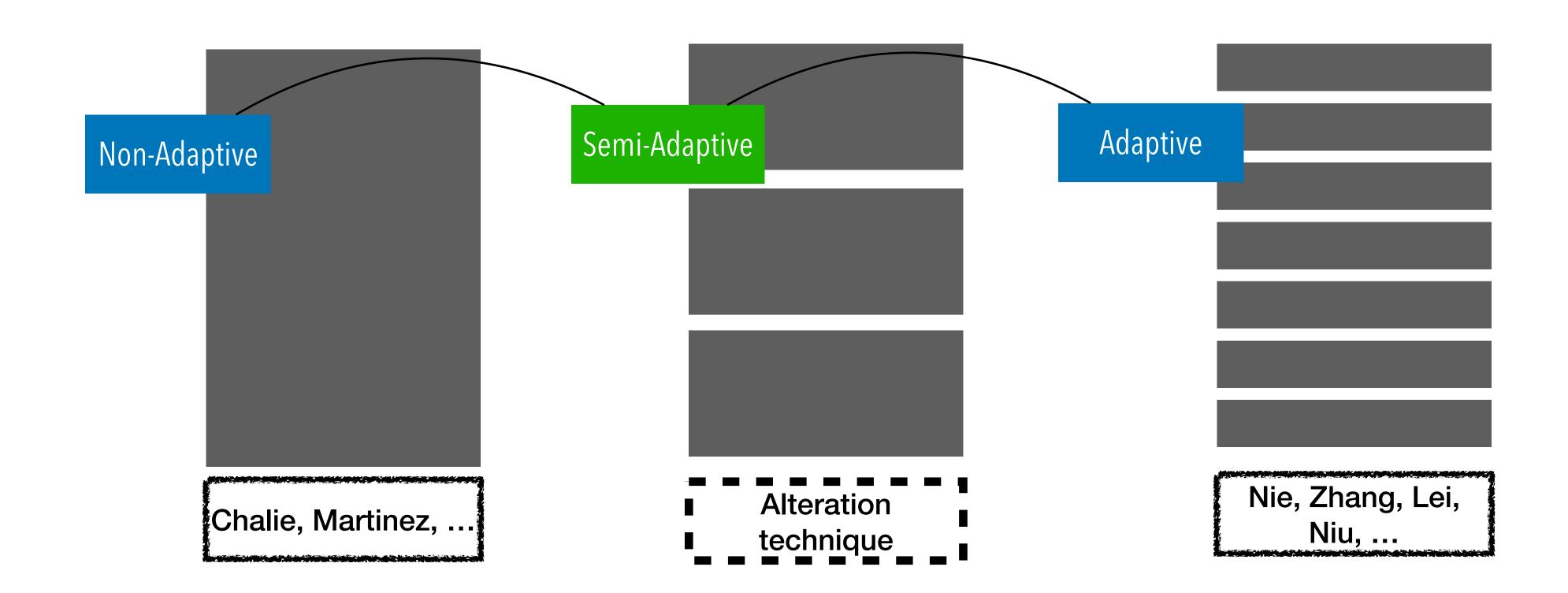




• 构建一个统一的故障定位理论和框架



• 构建一个统一的故障定位理论和框架







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